

# Impact of Numerics on Stratospheric Transport

Insights from Theory, Idealized and Comprehensive\* Models

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<sup>1</sup> Stanford University

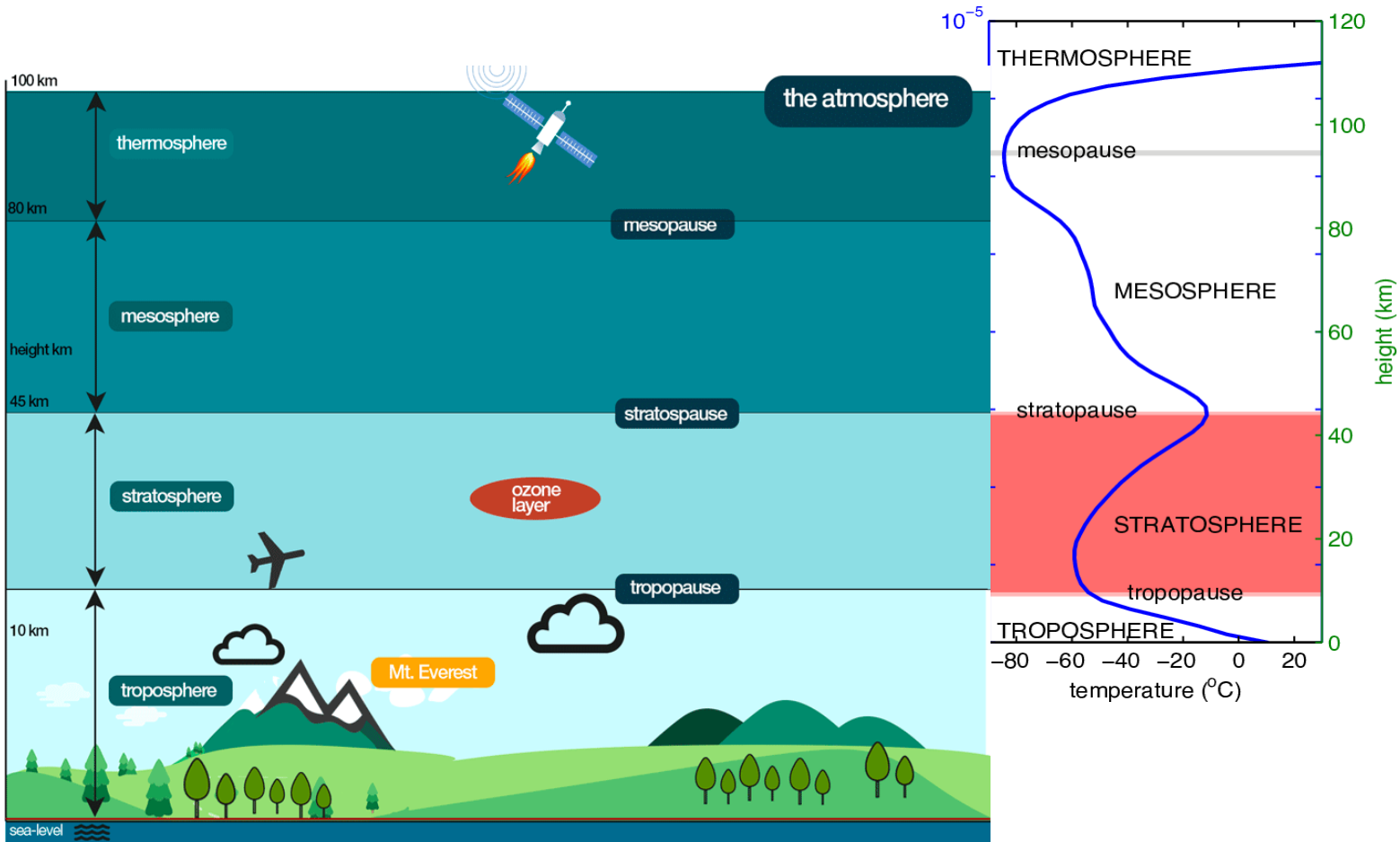
<sup>2</sup> Courant Institute of Mathematical Sciences, New York University

<sup>3</sup> Ludwig Maximilian University, Munich, Germany

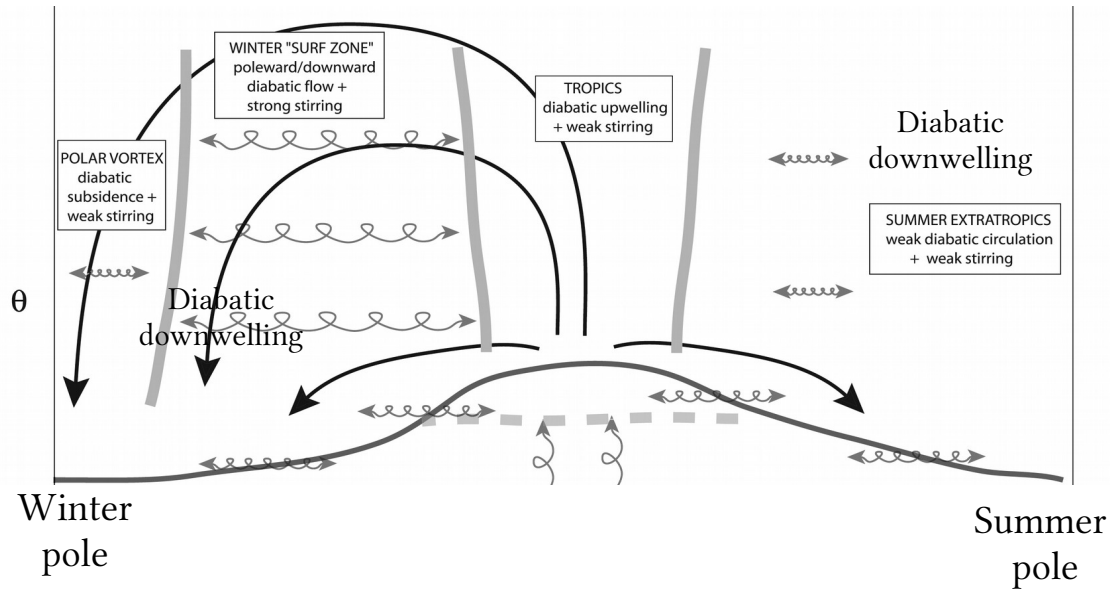
<sup>4</sup> Massachusetts Institute of Technology

<sup>5</sup> Harvard University

<sup>6</sup> National Center for Atmospheric Research



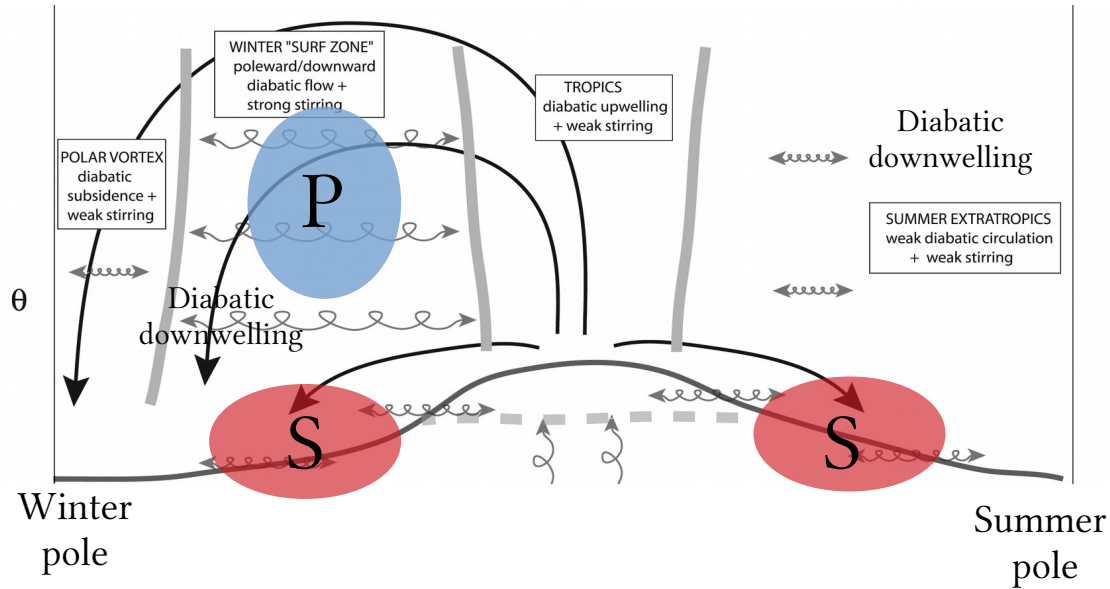
# Large-Scale (wave-driven) Circulation of the Stratosphere a.k.a. BDC



(Figure: Marianna Linz)

- Brewer-Dobson Circulation (BDC) is **wave-driven**
- Tropical upwelling, extratropical downwelling of mass

# Large-Scale (wave-driven) Circulation of the Stratosphere a.k.a. BDC

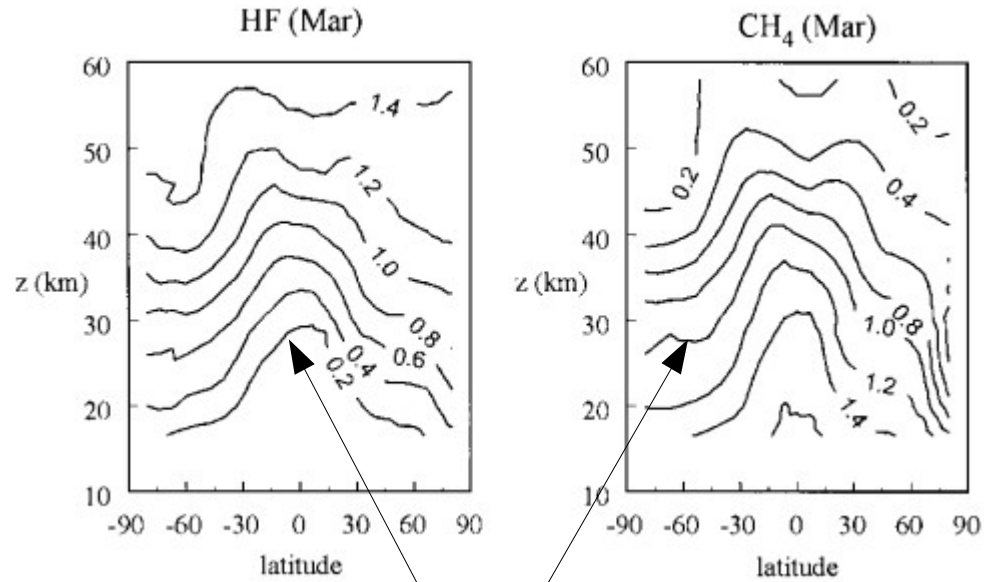


P : planetary-scale wave drag  
S : synoptic-scale wave drag

(Figure: Marianna Linz)

- Brewer-Dobson Circulation (BDC) is **wave-driven**
- Tropical upwelling, extratropical downwelling of mass
- Winter midlatitude “surf zone” driven by planetary wave breaking
- Quiescent summer hemisphere

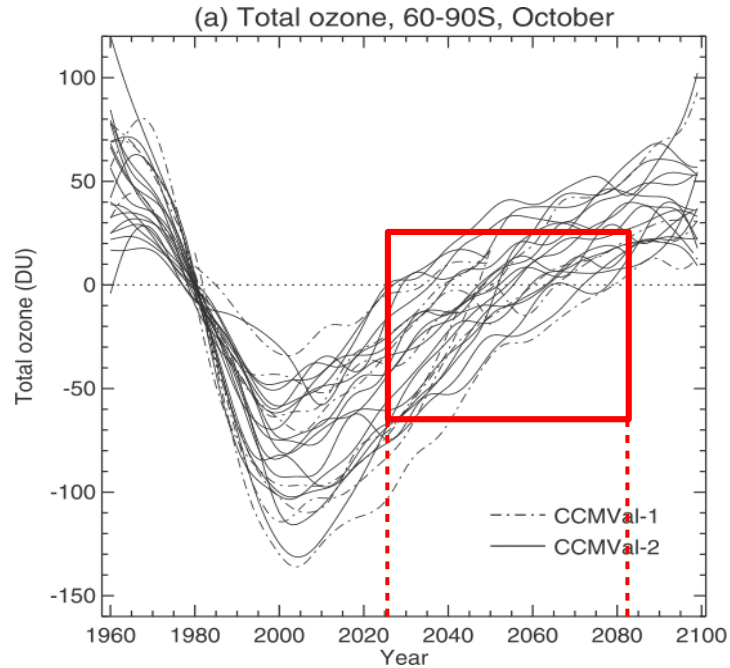
# Large-Scale circulation (more so than chemistry) determines trace gas distribution



(Figure: Plumb 2002)

Similar contours for two trace gases **despite** different sources/sinks and opposite gradients

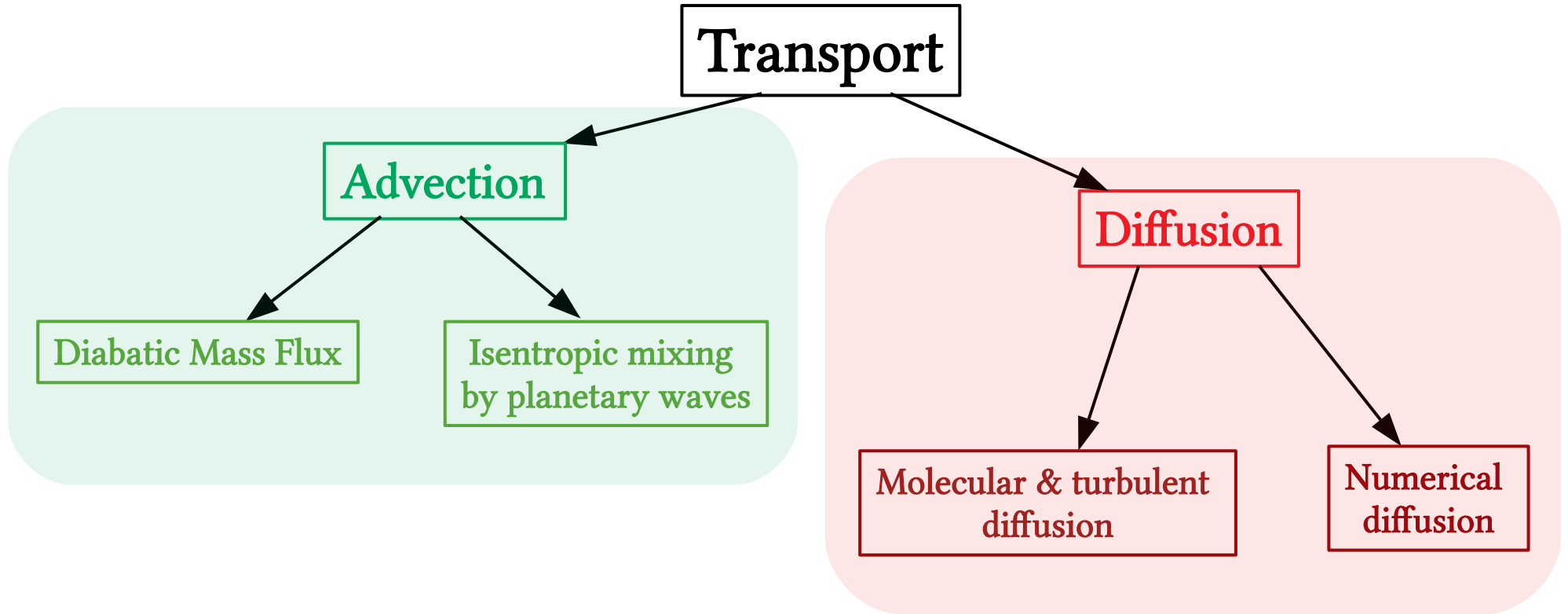
## Spread in ozone recovery projections: differences rooted in simulated transport



- A spread of over 60 years in ozone recovery times among state-of-the-art models.
- Differences correlated strongest with transport, not chemistry (Karpechko et al. 2013)
- Inaccuracies in ozone recovery essentially a transport problem!

Fig : Model projections of ozone recovery (from Karpechko et al. 2013)

# Various Processes Influence Stratospheric Transport



## Age-of-air: an idealized tracer to assess transport

- Age of air of an air-mass quantifies the time elapsed last surface contact. (Hall and Plumb 1994, Waugh and Hall '02)
- **A measure of transport timescales** in the atmosphere
- Age is an idealized tracer with a source in time. **Independent of chemistry/parameterizations, only depends on the tracer advection suite of a model.**

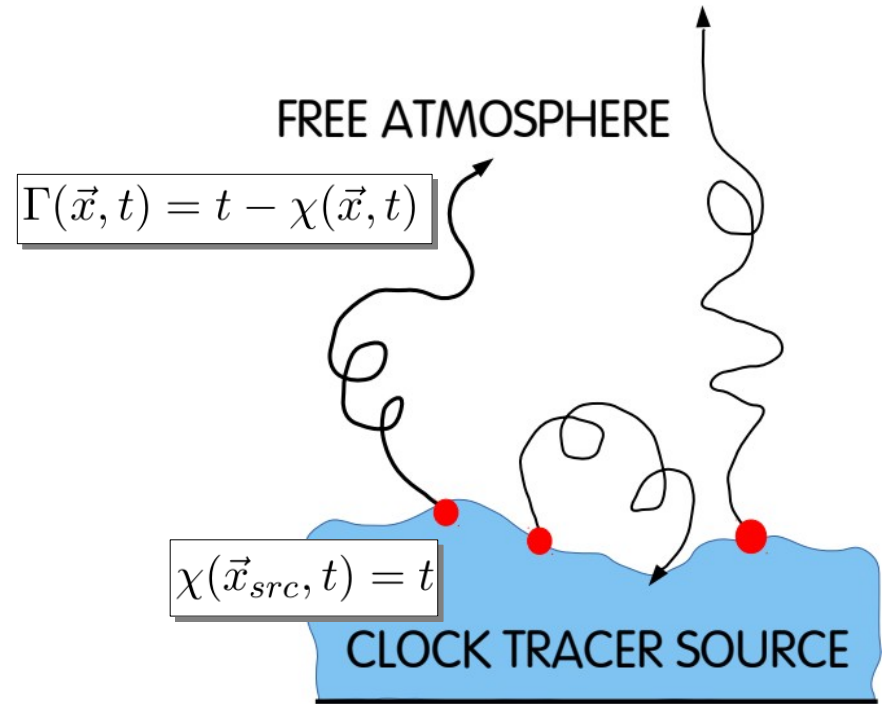
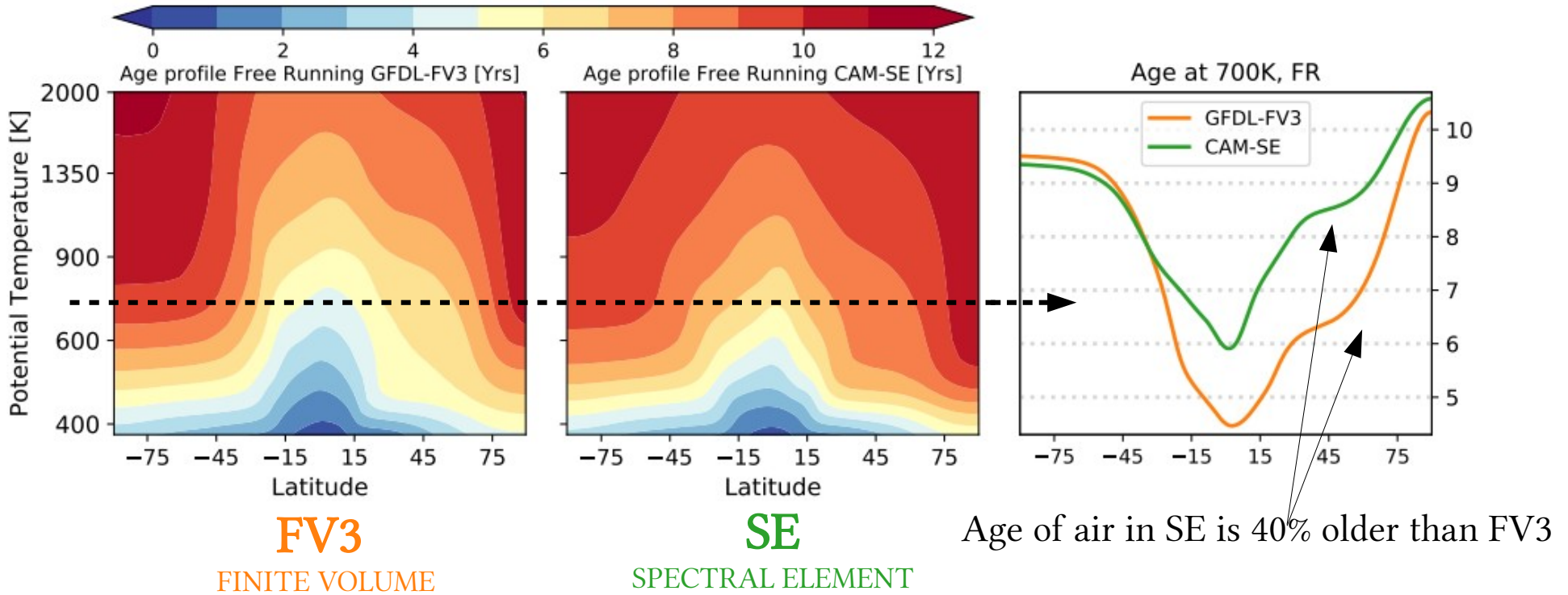


Fig: Computing age in models using clock tracer

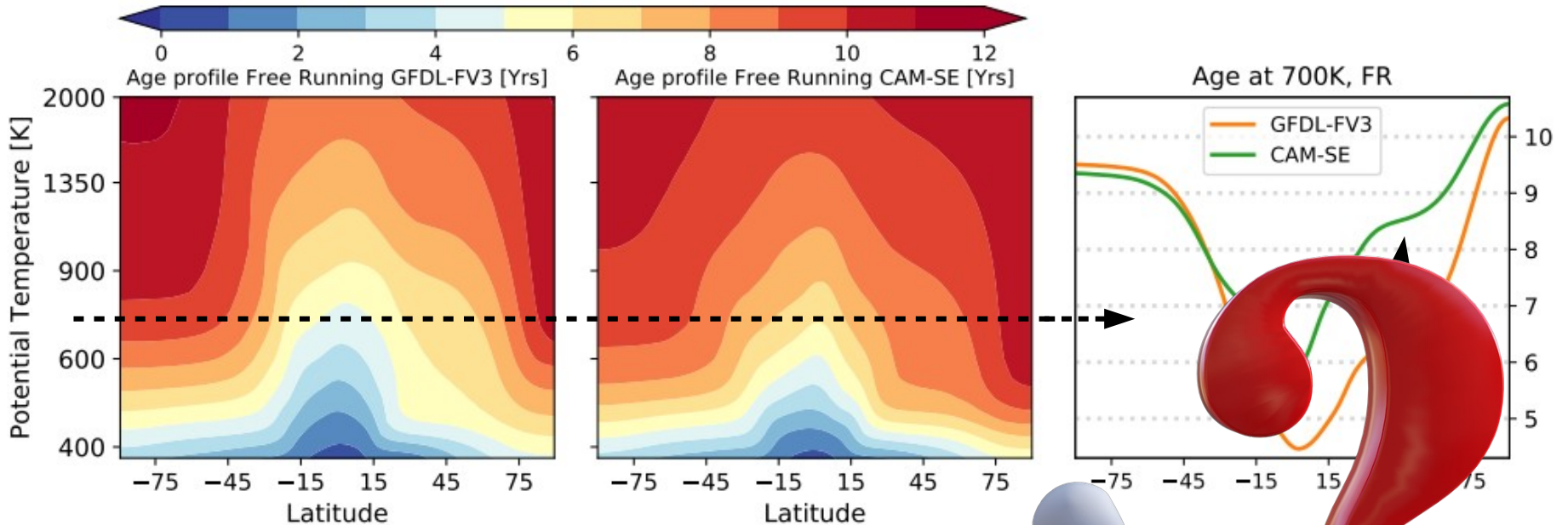


# Even two of the most modern dynamical cores exhibit very different transport!



Transport differences obtained at the “dynamical core level”

# Even two of the most modern dynamical cores exhibit very different transport!



**FV3**

FINITE VOLUME

**SE**

SPECTRAL ELEMENT

Age of air in SE is 10% older than FV3

Transport differences obtained at the “dynamical core level”



# A transport benchmark test to assess transport in different dynamical cores

A Proposal for the  
Intercomparison of the  
Dynamical Cores of Atmospheric  
General Circulation Models

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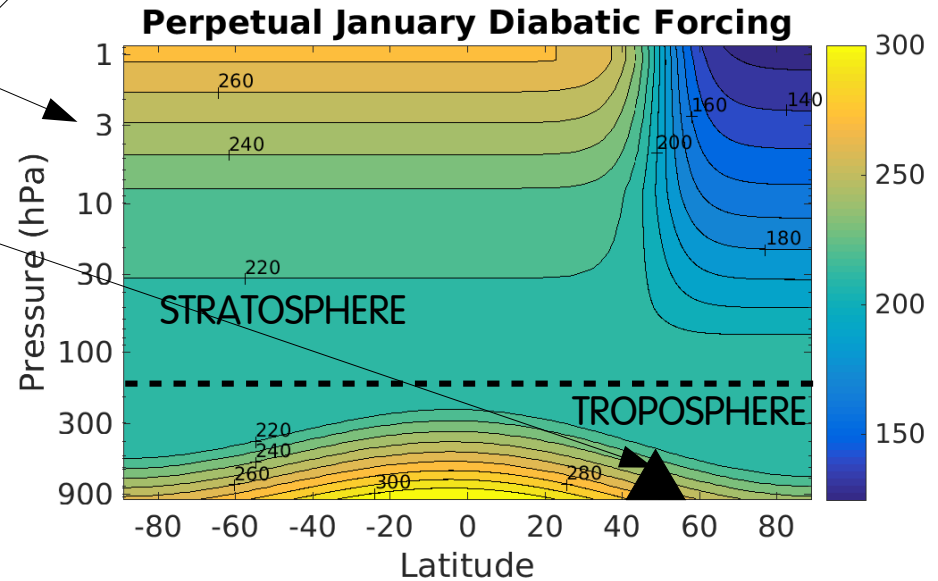
Isaac M. Held\*  
and Max J. Suarez\*\*

1994

## Configuration of the Benchmark test: **Dynamics**

- We build upon the Held-Suarez benchmark test for model dynamics
- Dynamics: Impose Held-Suarez + Polvani-Kushner type diabatic forcing i.e.,
  - + Short-wave heating → Newtonian relaxation to prescribed temperature profile
  - + PBL → Rayleigh damping
  - + GW dissipation → model sponge
  - + Stationary wave forcing → wave-2 topography
- Focus on large-scale dynamics and transport coupling. **No uncertainty from parameterizations.**

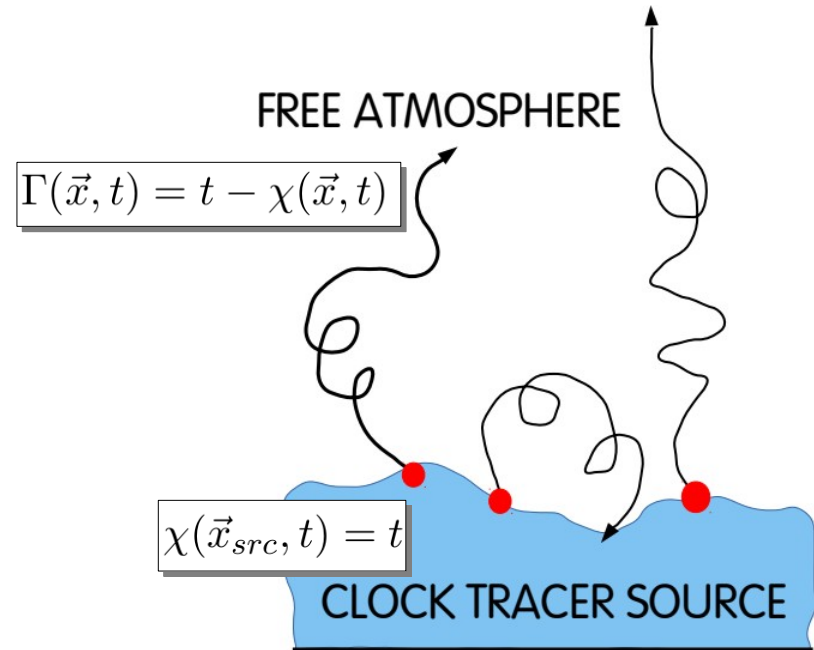
$$\frac{\partial T}{\partial t} = \dots - k_T(\phi, \sigma) [T - T_{eq}(\phi, \rho)]$$



Held-Suarez + Polvani-Kushner (HSPK) setup

## Configuration of the Benchmark test: **Transport**

- Transport: use a **clock tracer** at the surface to compute the age-of-air in idealized models
- Integrate models for 10,000 model days with **no seasonal cycle – perpetual January conditions**
- We call this – the **Free Running (FR) test**



Quantifying transport in models using clock tracer

We benchmark 4 dynamical cores from 2 modeling centers ...

↓ Spectral-methods based

**GFDL-PS**  
PSEUDOSPECTRAL

↓ Finite Volume based

**CAM-FV**  
CAM FINITE VOLUME

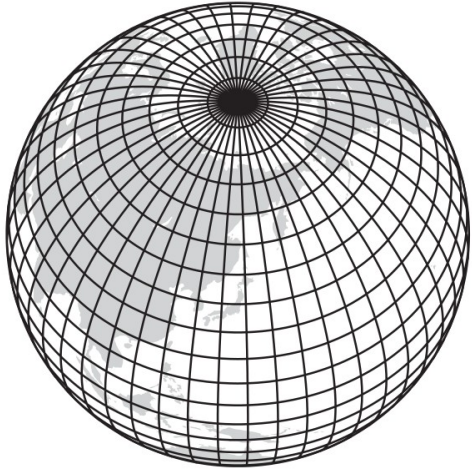
← Traditional cores

**CAM-SE**  
CAM SPECTRAL ELEMENT

**GFDL-FV3**  
CUBED SPHERE FINITE VOLUME

← Modern cores

LATITUDE-LONGITUDE GRID

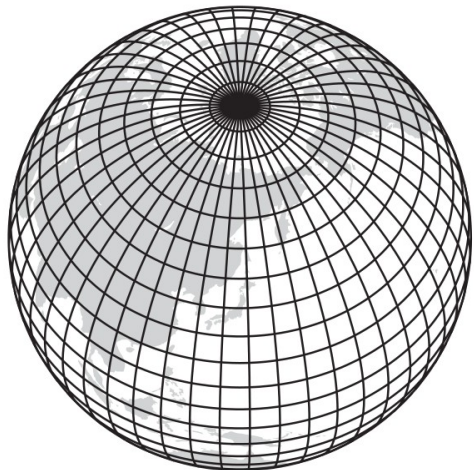


**CAM-FV**

CAM FINITE VOLUME

Differences in  
numerical grids

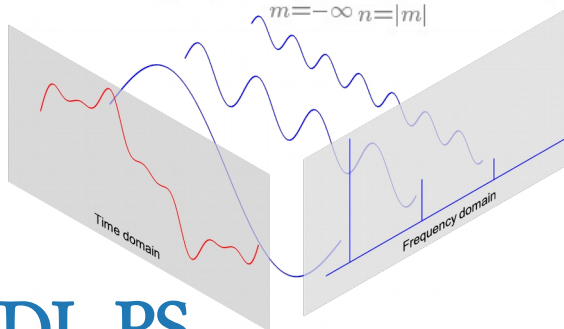
LATITUDE-LONGITUDE GRID



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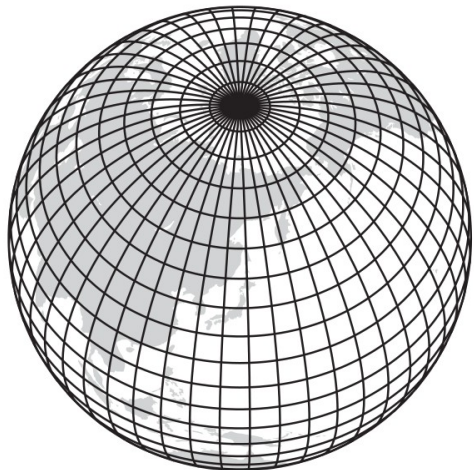
$$f(\theta, \phi) = \sum_{m=-\infty}^{\infty} \sum_{n=|m|}^{\infty} f_{mn} P_{mn}(\cos \theta) e^{im\phi}$$



**GFDL-PS**  
PSEUDOSPECTRAL



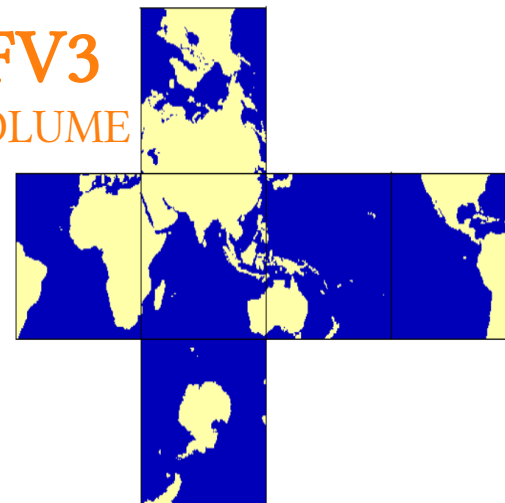
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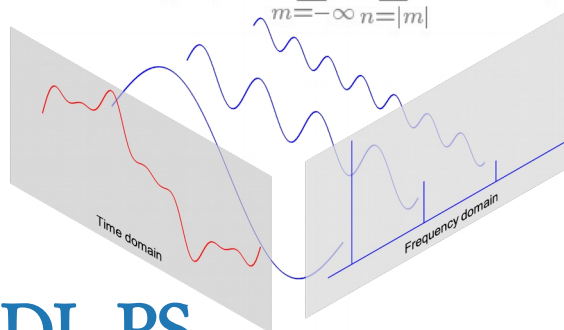
**GFDL-FV3**

CUBED SPHERE FINITE VOLUME



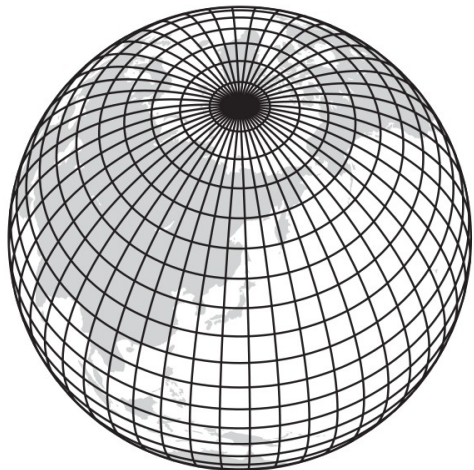
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**GFDL-PS**  
PSEUDOSPECTRAL

LATITUDE-LONGITUDE GRID

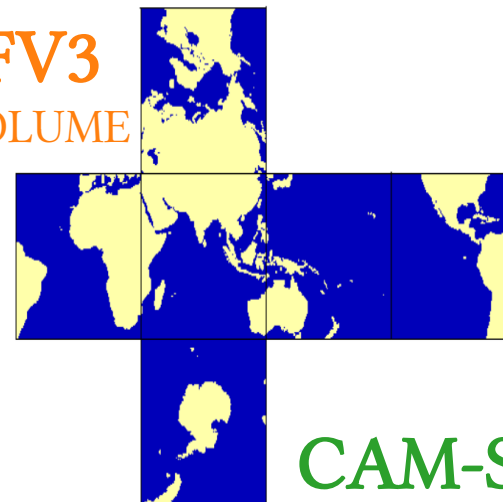


**CAM-FV**  
CAM FINITE VOLUME

**GFDL-FV3**

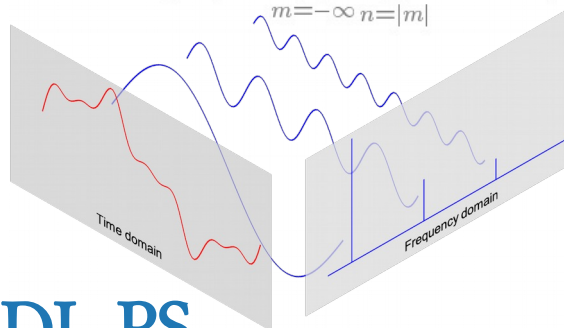
CUBED SPHERE FINITE VOLUME

Differences in  
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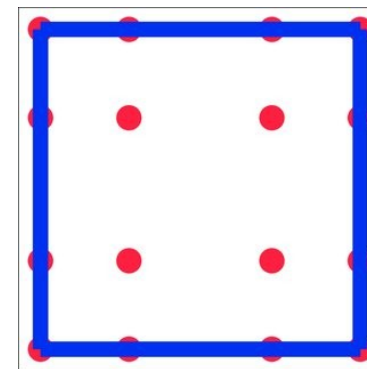
**CAM-SE**  
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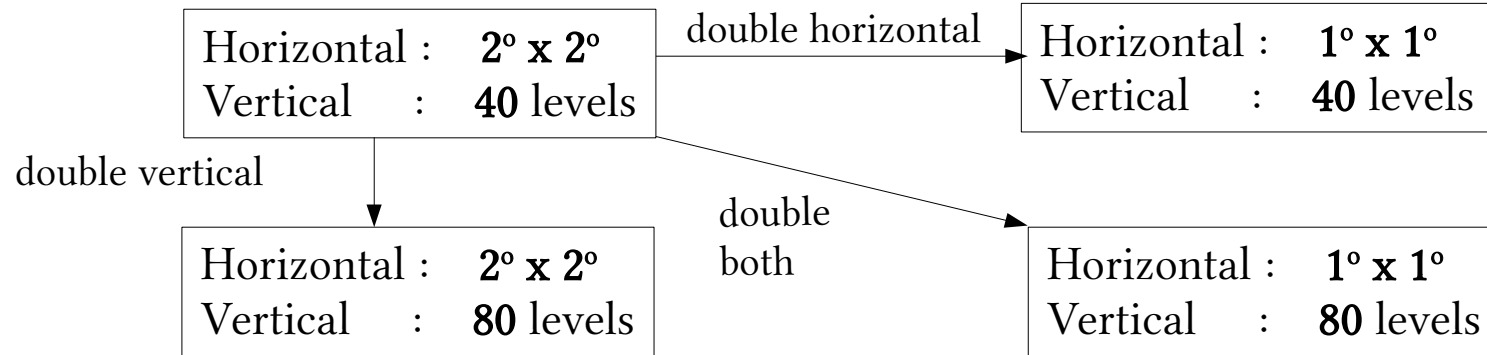


**GFDL-PS**  
PSEUDOSPECTRAL

+

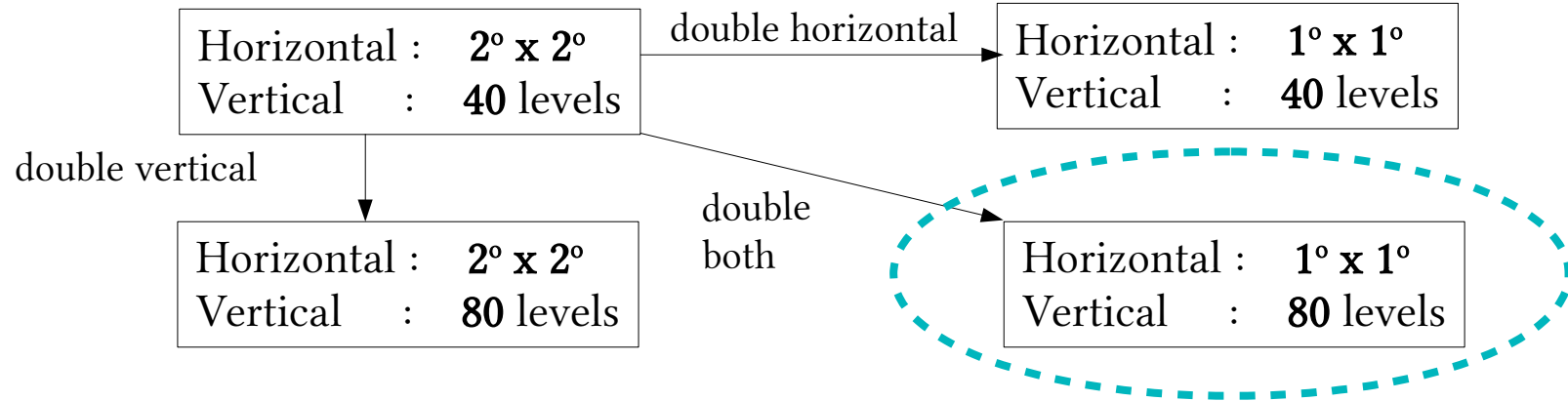


... and test the sensitivity of simulated transport to grid resolution as well



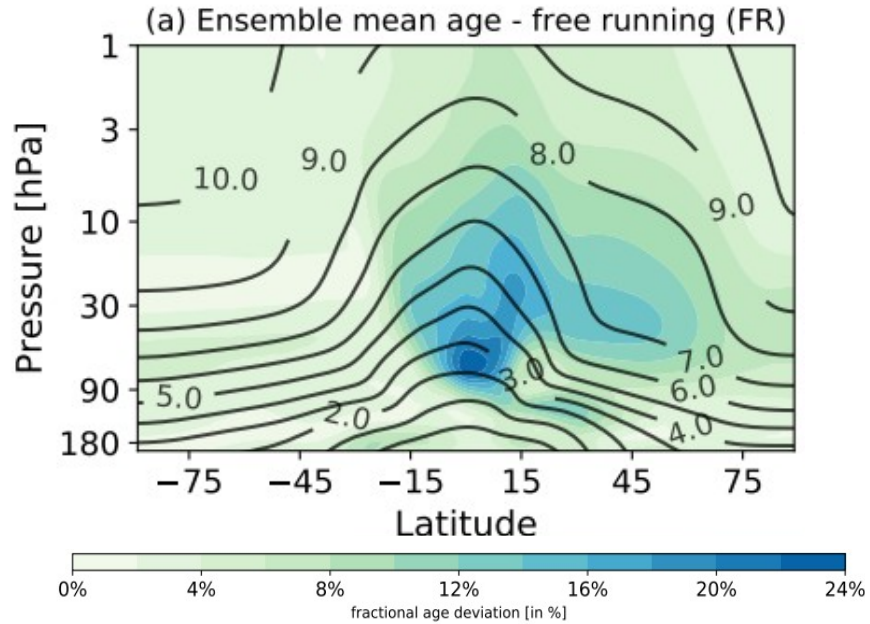
Million+ core hours on Cheyenne. 60+ terabytes (!) of data.

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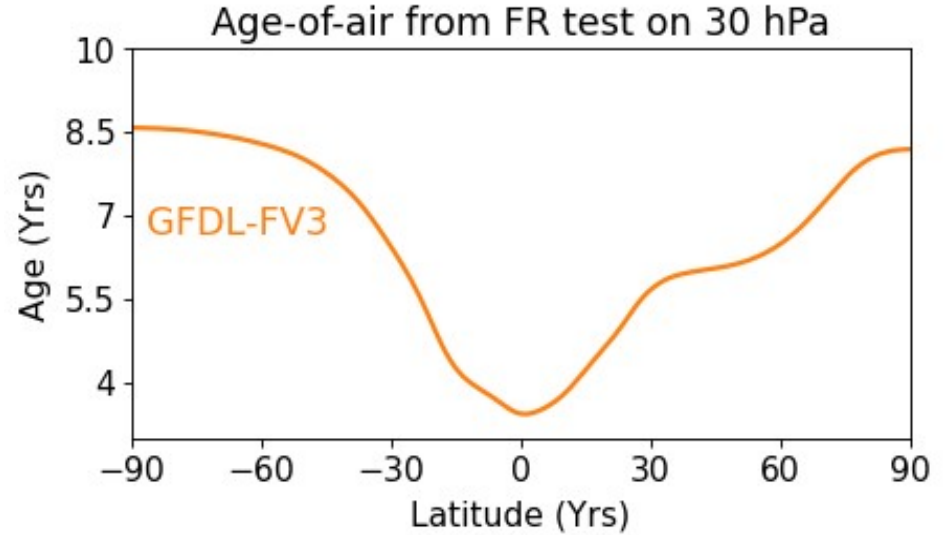
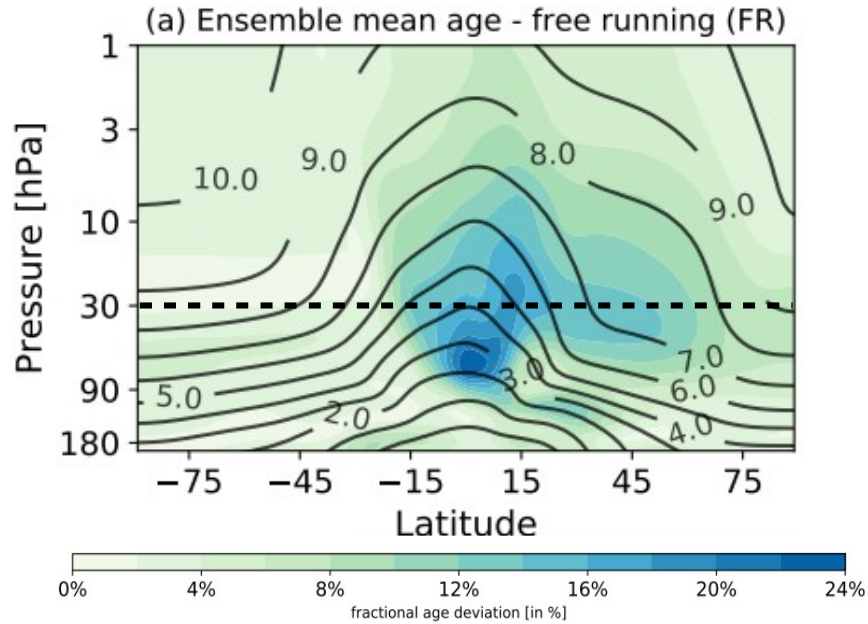
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# Age-of-air from the Free Running (FR) benchmark test



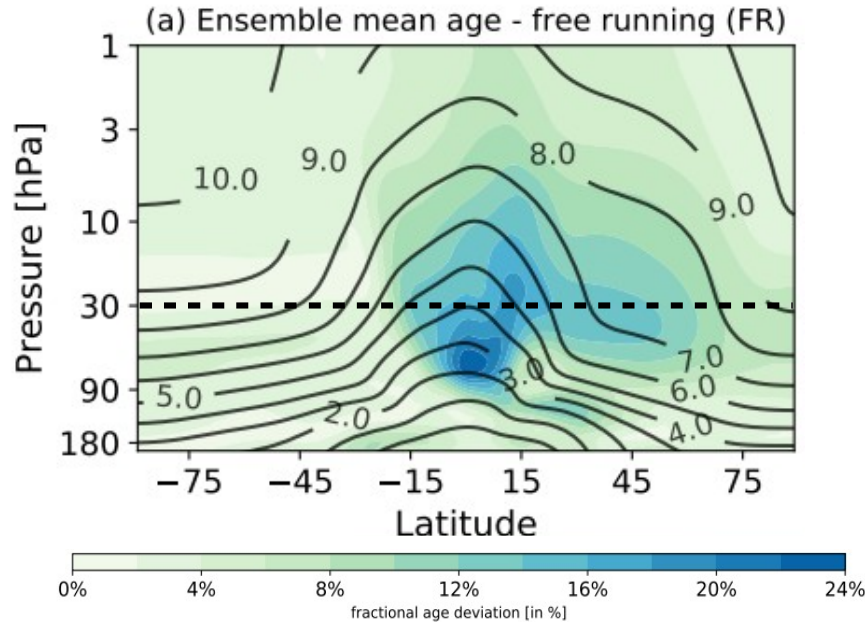
Intermodel age differences strongest in the tropics

# Age-of-air from the Free Running (FR) benchmark test

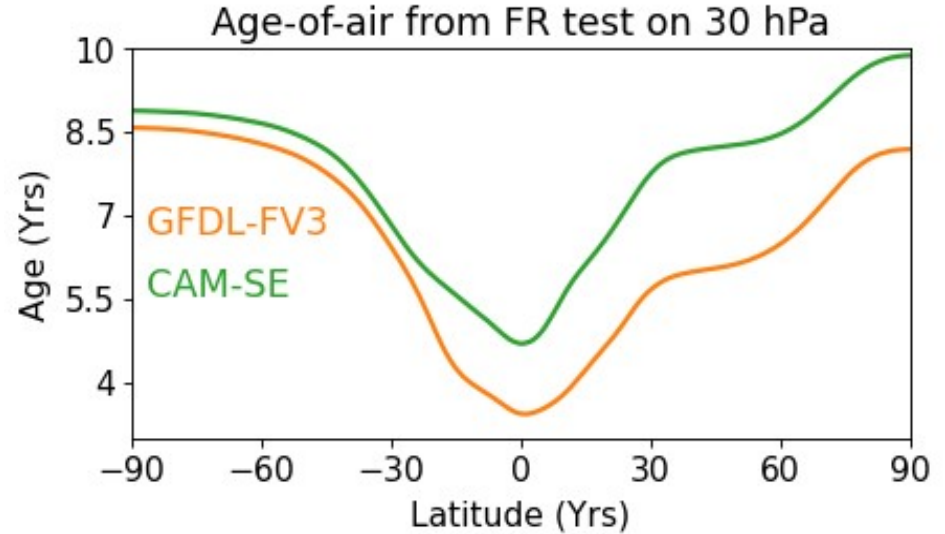


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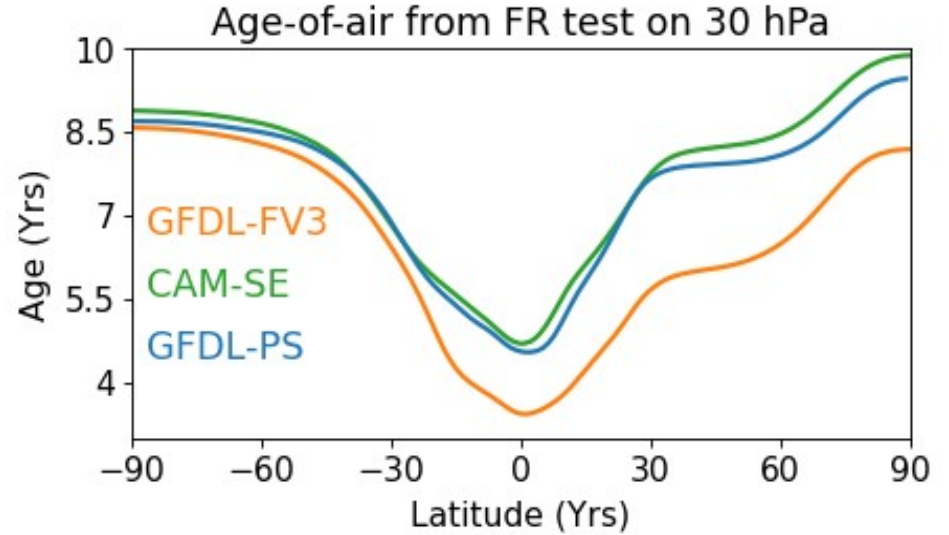
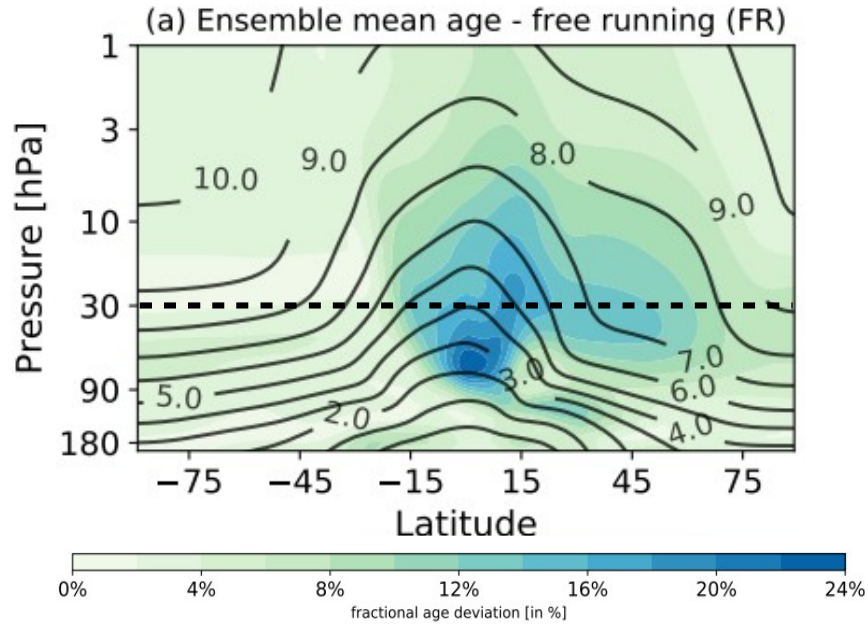


Intermodel age differences strongest in the tropics



Striking differences in age between GFDL-FV3 and CAM-SE

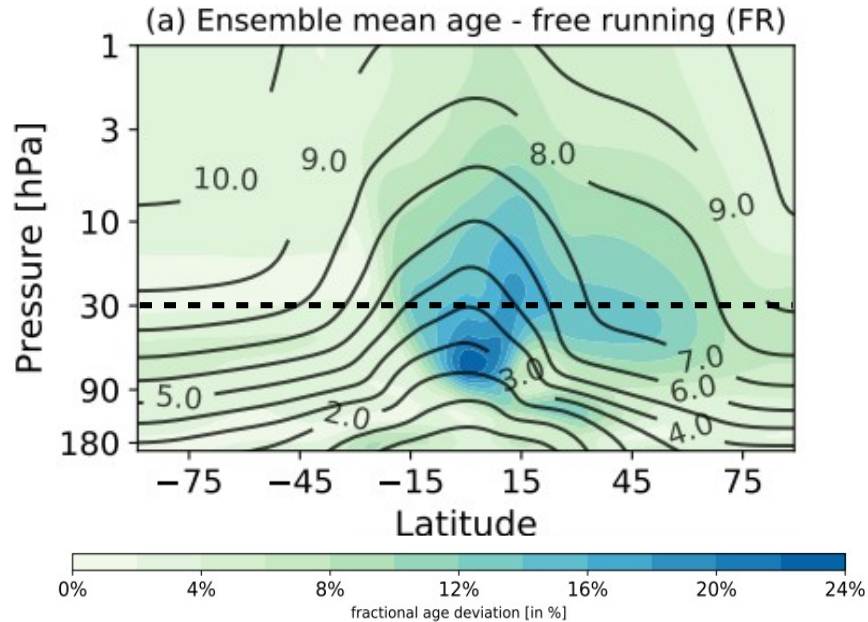
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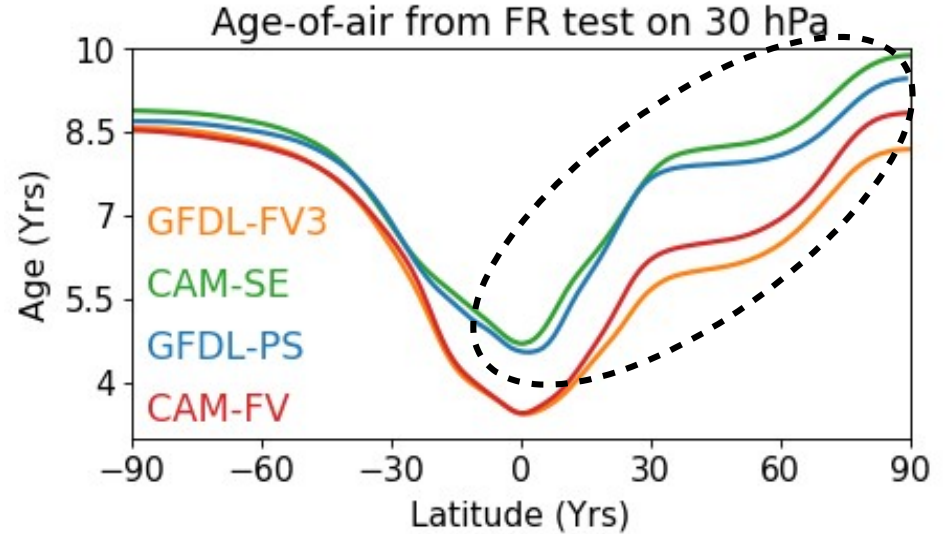
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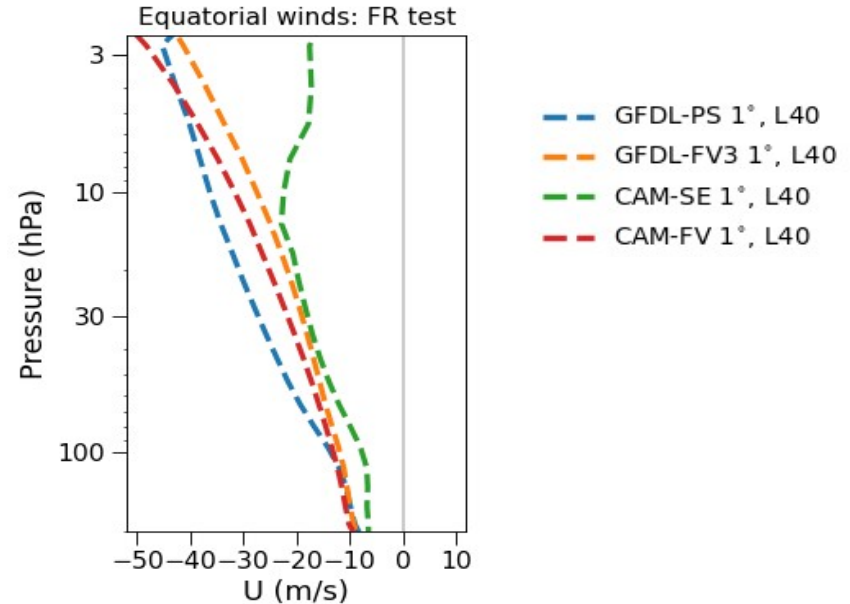
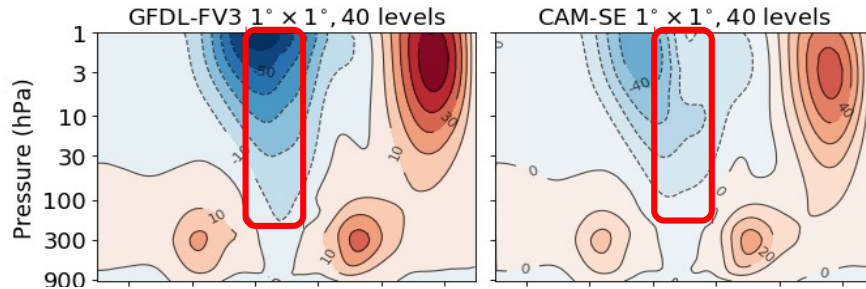


Intermodel age differences strongest in the tropics



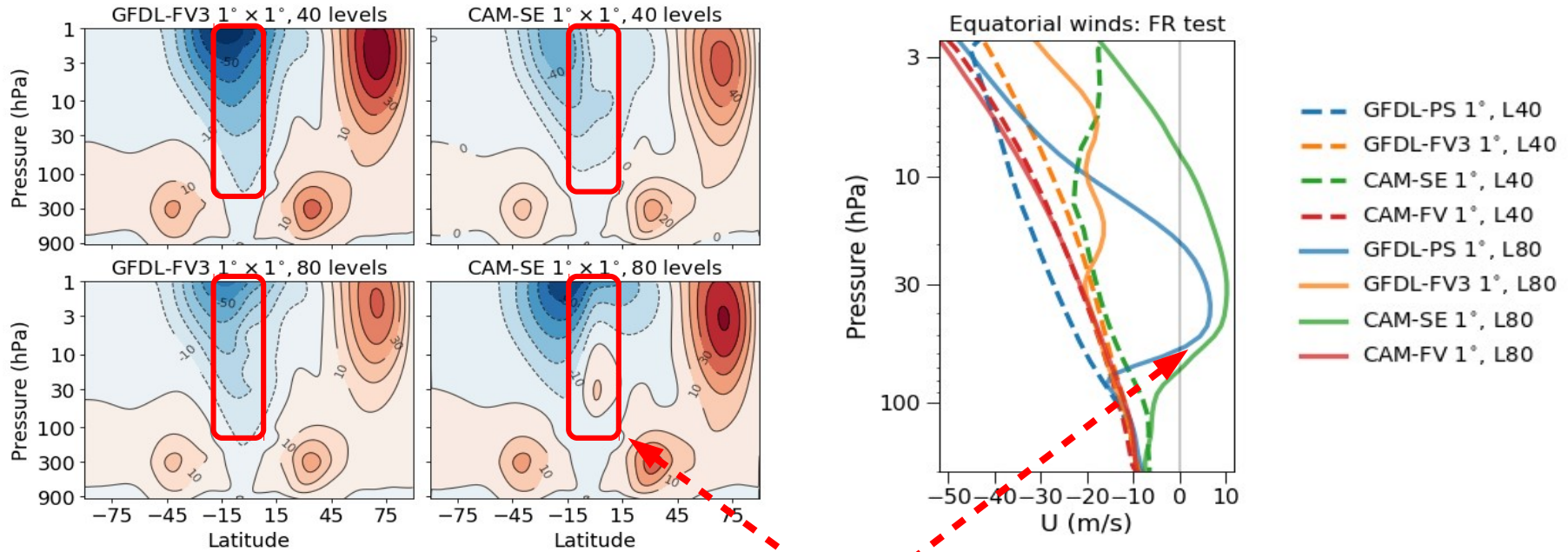
Striking differences in age between finite-volume and spectral-based cores

## The dynamical cores **fail** the Held-Suarez test in the stratosphere



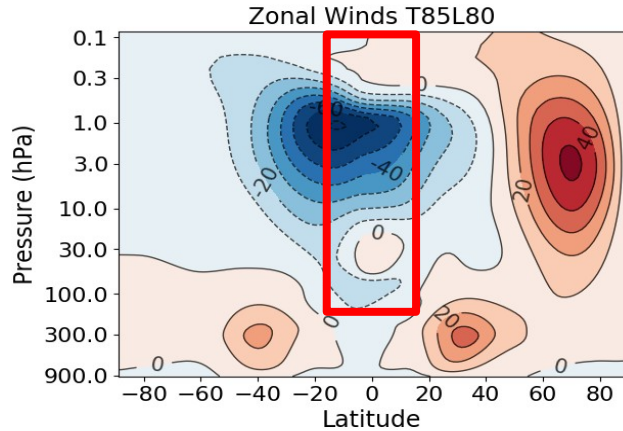
- The dynamical cores disagree on the tropical stratospheric winds.
- **Dichotomy** among finite volume (tropical easterly) and spectral-based (tropical westerly) dycores **at high vertical resolution**.
- Differences in tropical dynamics lead to global differences in transport.

# The dynamical cores **fail** the Held-Suarez test in the stratosphere

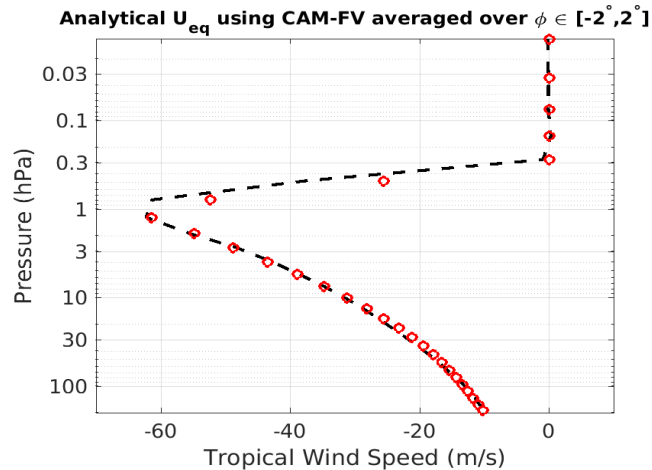


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# Updating our benchmark test: specifying the tropical winds

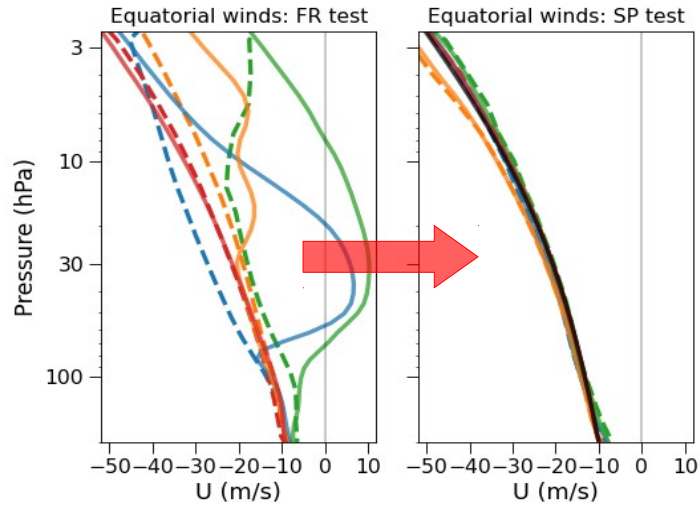


$$u_t(\lambda, \phi, p, t) = - \frac{[u(\lambda, \phi, p, t) - u_{eq}(p)]}{\tau}$$



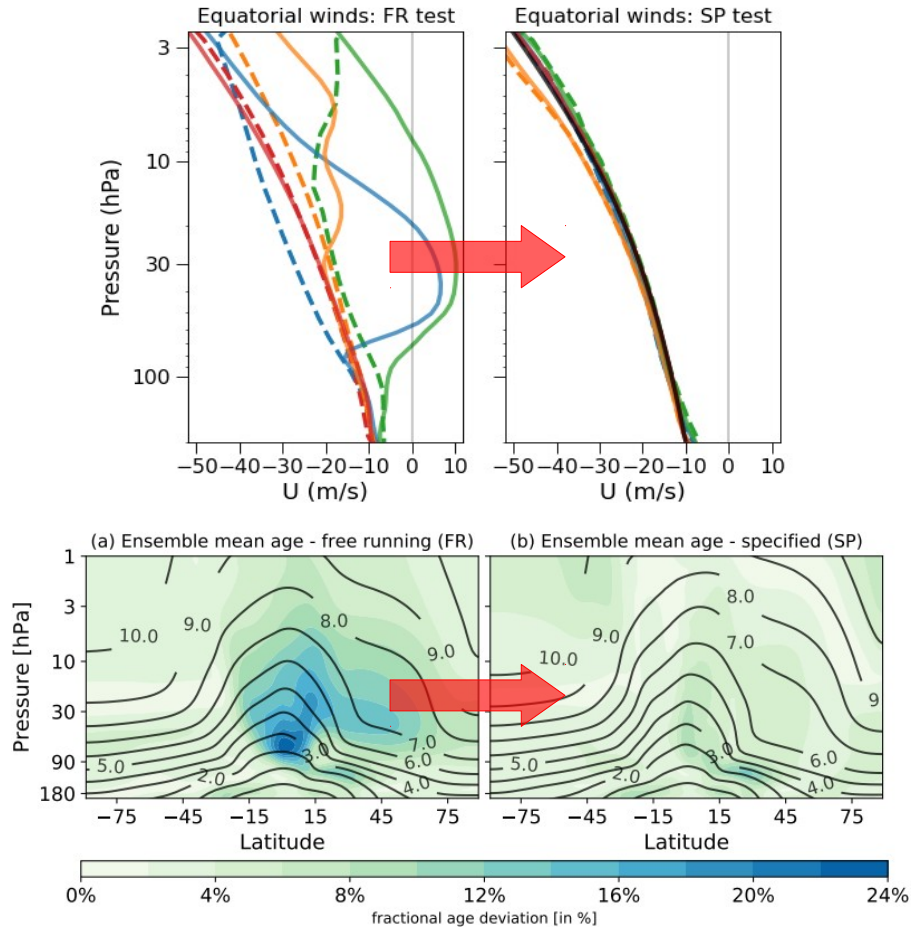
- **Analytical  $U_{eq}(p)$  profile:** Specified winds in the tropical stratosphere to compensate for unresolved small-scale processes. Inspired by specified QBO in WACCM.
- Newtonian relaxation to this prescribed easterly wind profile
- We call this - the **Specified (SP) test**

## Consistent tropical dynamics under the nudged (SP) benchmark test



- Nudging eliminates tropical wind variance among dynamical cores, and across resolutions

# Consistent tropical dynamics under the nudged (SP) benchmark test

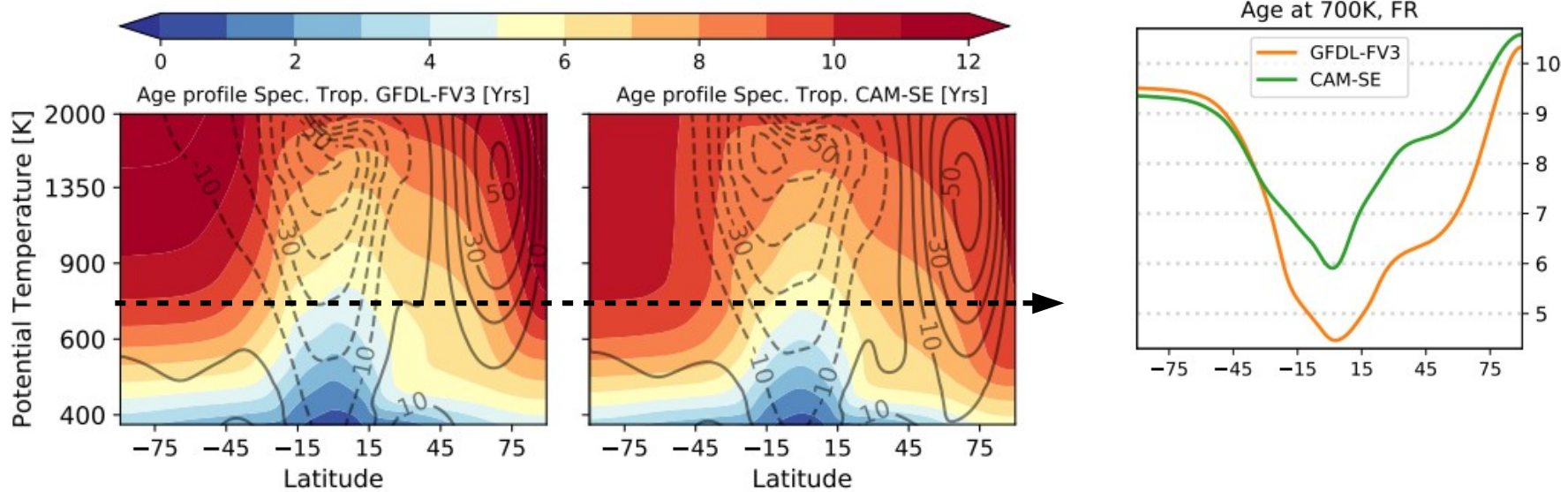


- Nudging eliminates tropical wind variance among dynamical cores, and across resolutions

- Reduction in tropical wind variance leads to significant reduction in ensemble age variance

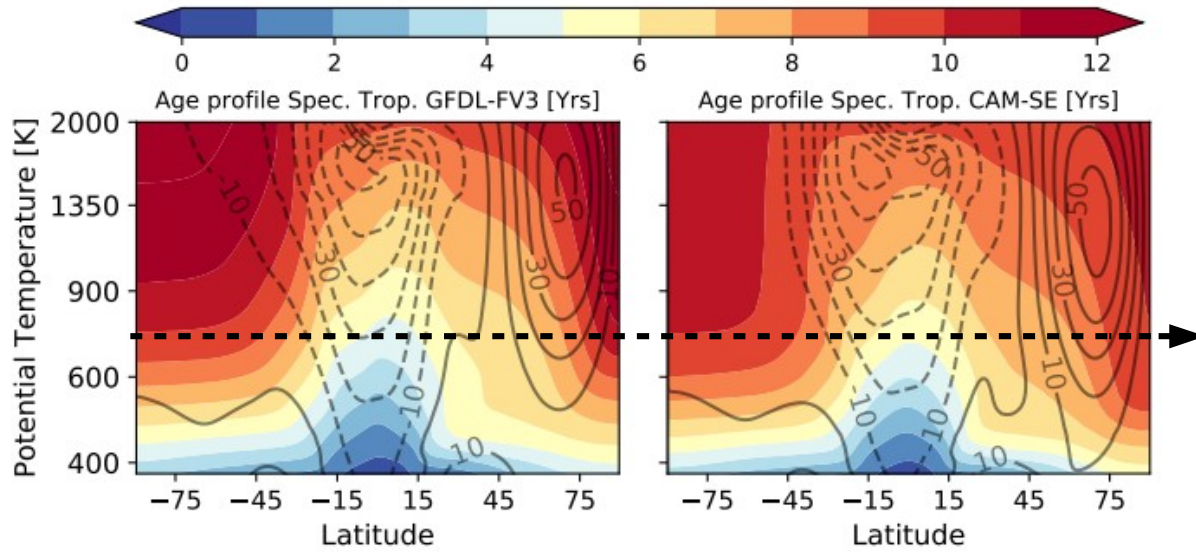


# Does constraining the tropical winds resolve the issue?

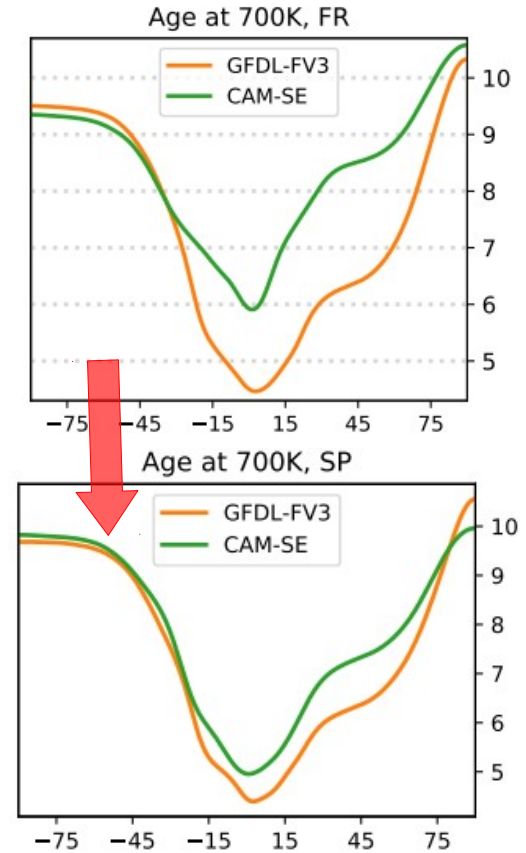


Constraining tropical winds among models drastically reduces the age difference. Some differences still remain.

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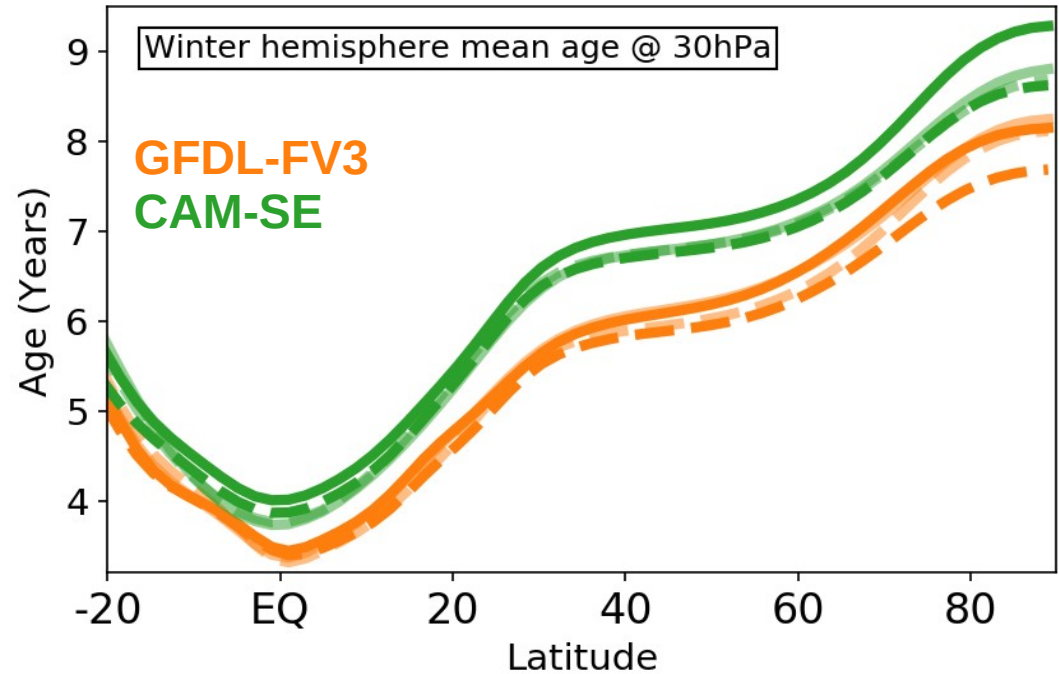




## Models show signs of convergence under the nudged (SP) benchmark test

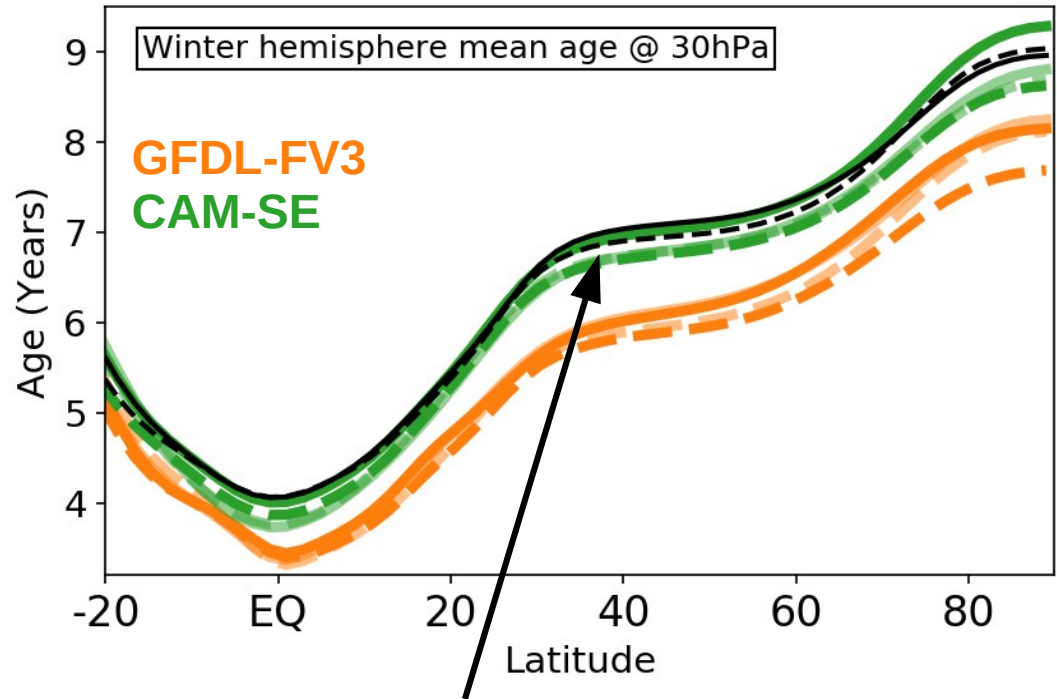
However, the age-of-air in both the models converges to different values

Highlights the strong tropical control of stratospheric transport.



## Models show signs of convergence under the nudged (SP) benchmark test

We test the **spectral element core** at even higher horizontal and vertical resolutions

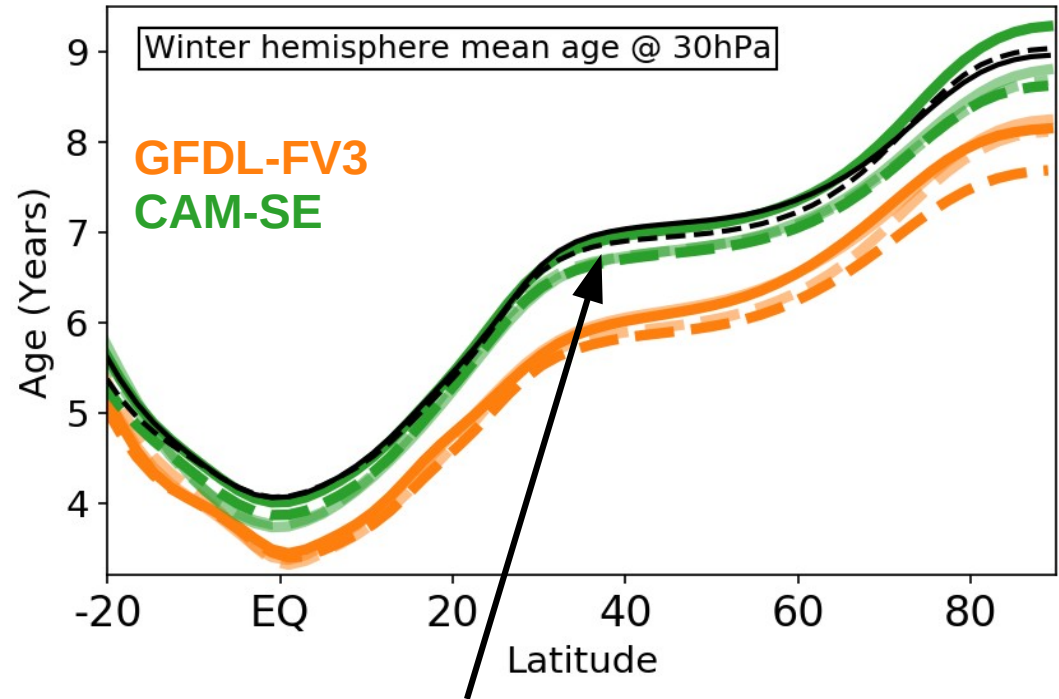


Black curves : HiRes CAM-SE runs  
0.5°, L80 (dashed) and 1°, L160 (solid)

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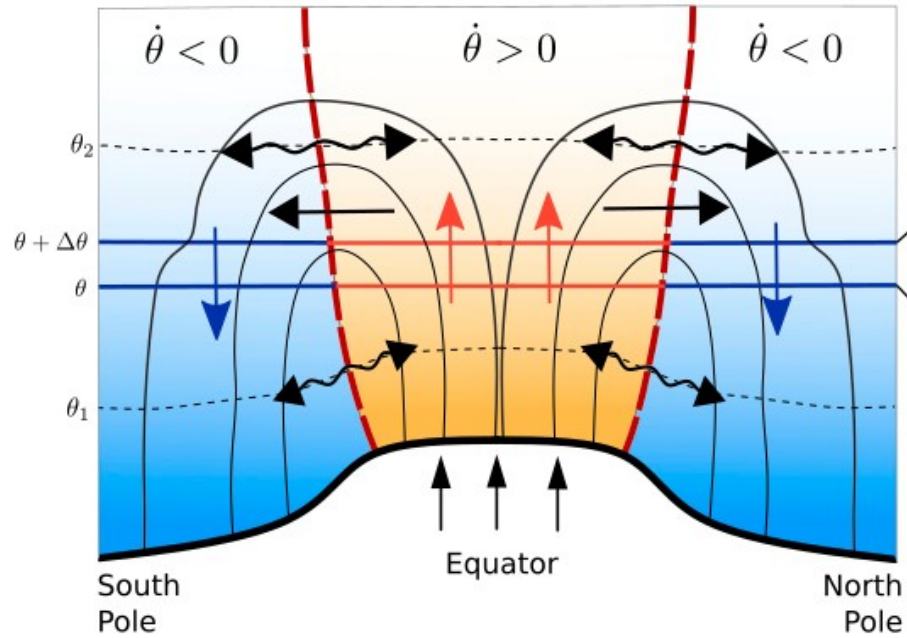
(not shown) Nudging GFDL-FV3 tropical winds to westerlies increases the age throughout the stratosphere.



Black curves : HiRes CAM-SE runs  
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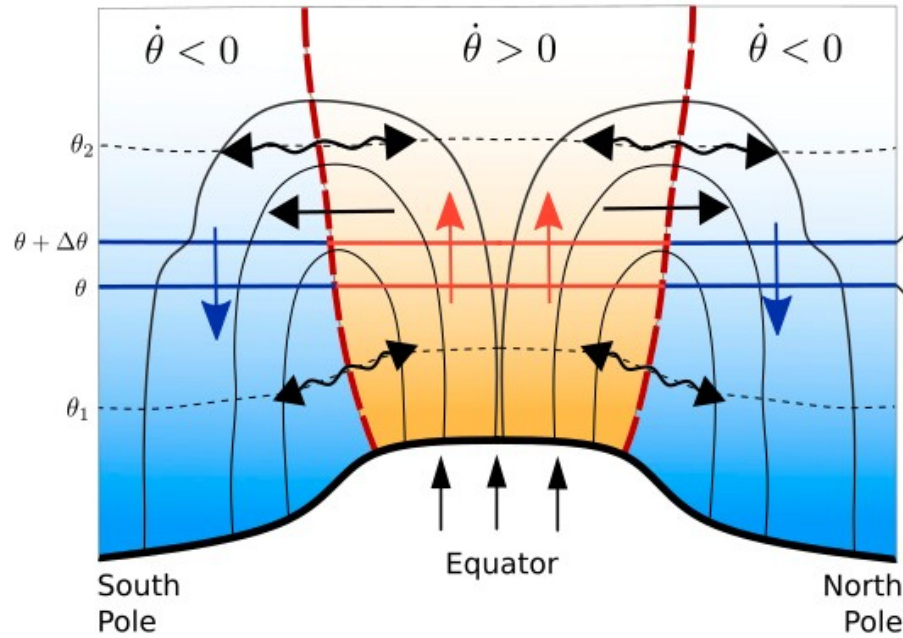
Using Conceptual Transport Models to Understanding Why  
Tropical Westerlies lead to Higher Age?

# Using the theoretical “leaky pipe” model to estimate midlatitude wave-induced mixing

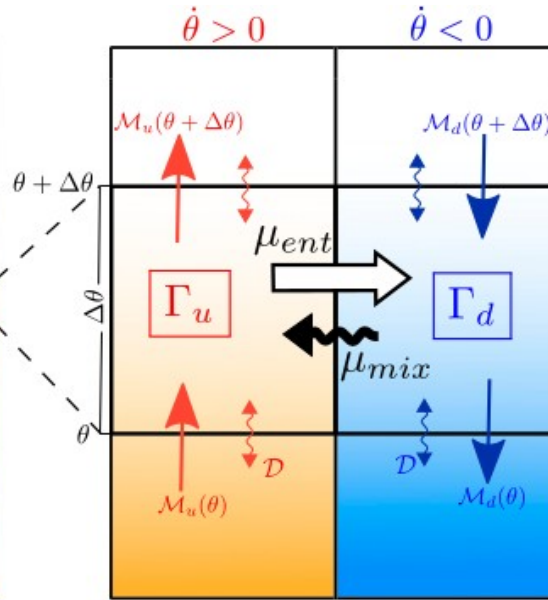


Full three-dimensional model transport

# Using the theoretical “leaky pipe” model to estimate midlatitude wave-induced mixing



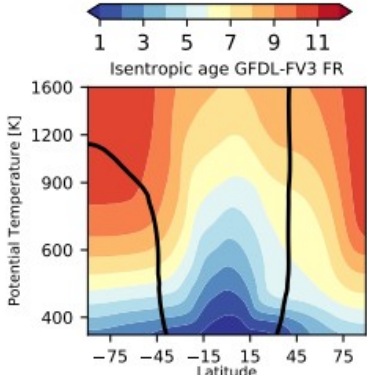
Full three-dimensional model transport



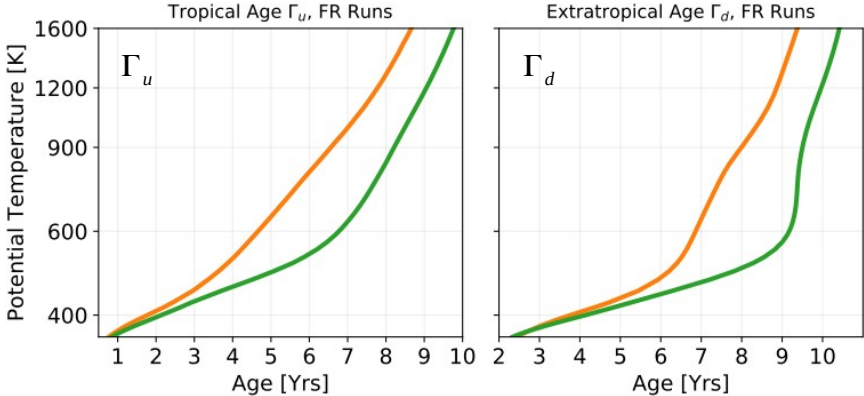
Transport as exchange between tropical and extratropical “pipes”

# Using theory to estimate mixing flux

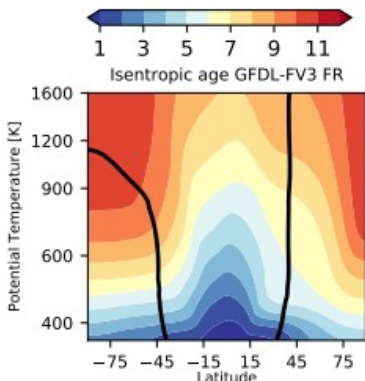
## Mass-flux weighted ages



Dimensional reduction from full model age



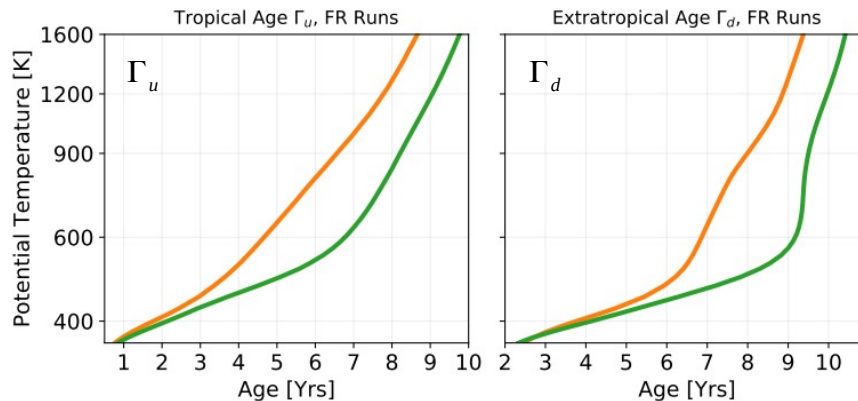
# Using theory to estimate mixing flux



Dimensional reduction from full model age



## Mass-flux weighted ages



In the no-diffusion limit, the vertical gradient of the average tropical age allows quantifying the mixing fluxes across the subtropical barrier (Linz et al. 2021)

Mixing equation :

$$\frac{\partial \Gamma_u}{\partial \theta} = \frac{\sigma}{\mathcal{M}} + \frac{\mu_{mix} \Delta \Gamma}{\mathcal{M}}$$

Advection term

Mixing term

$\mathcal{M}(\theta)$  : diabatic mass flux

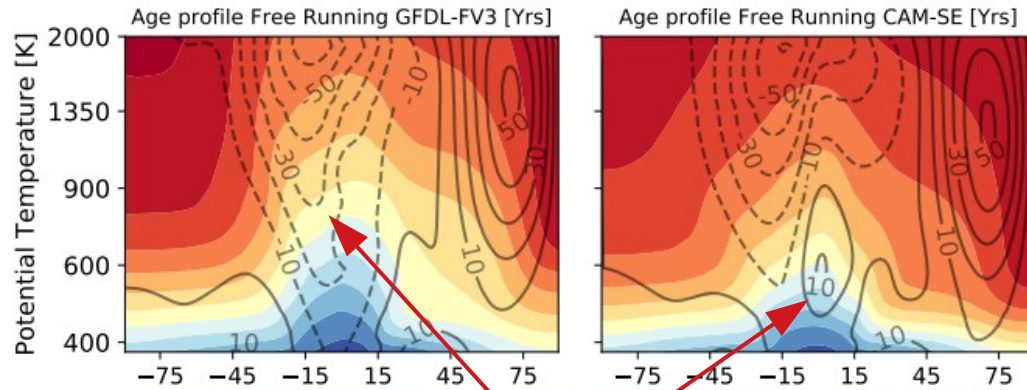
$\sigma(\theta)$  : horizontally avgd density

$\mu_{mix}(\theta)$  : ET  $\rightarrow$  T mixing flux

$\Delta \Gamma(\theta) = \Gamma_d(\theta) - \Gamma_u(\theta)$



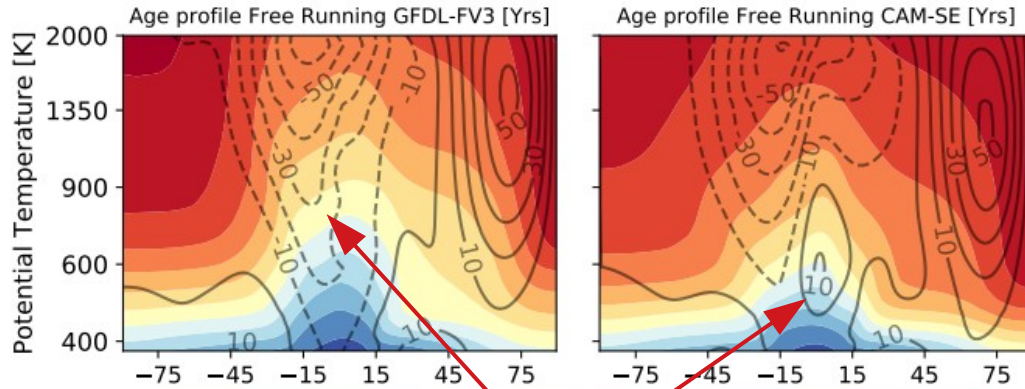
# Tropical Westerlies Induce Enhanced Tropical-Extratropical Trace Gas Mixing



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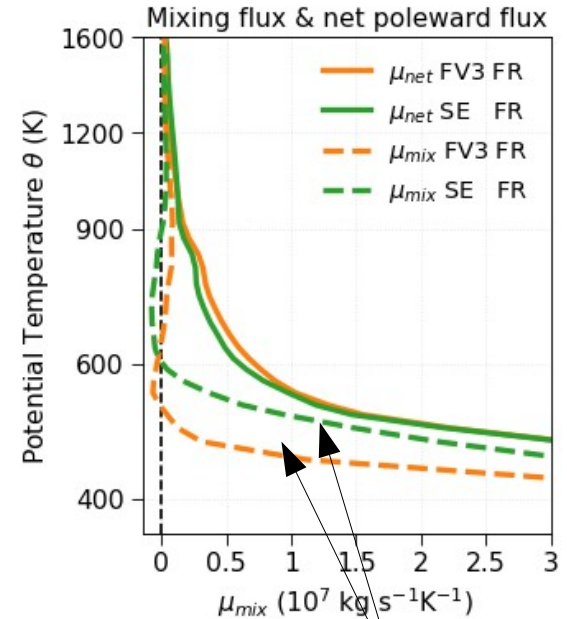
- The tropical winds in the two models have different phases. Akin to different phases of the QBO.
- Westerlies induce more mixing between the two regions by allowing the midlatitude mixing fluxes to percolate deeper into the tropics

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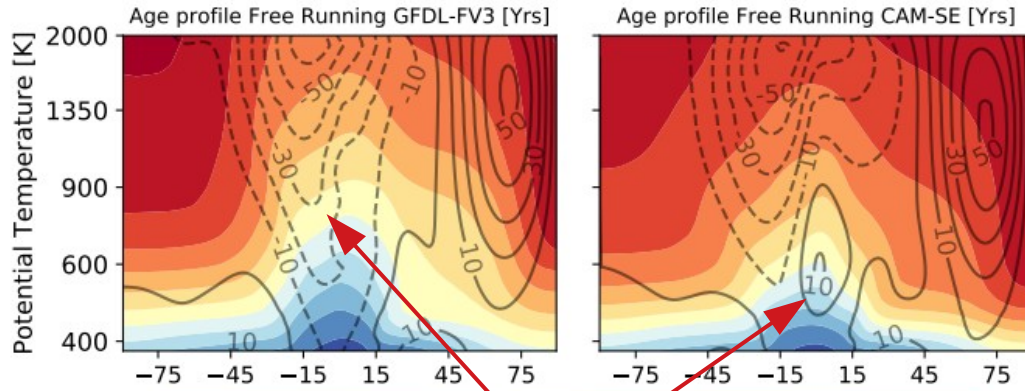
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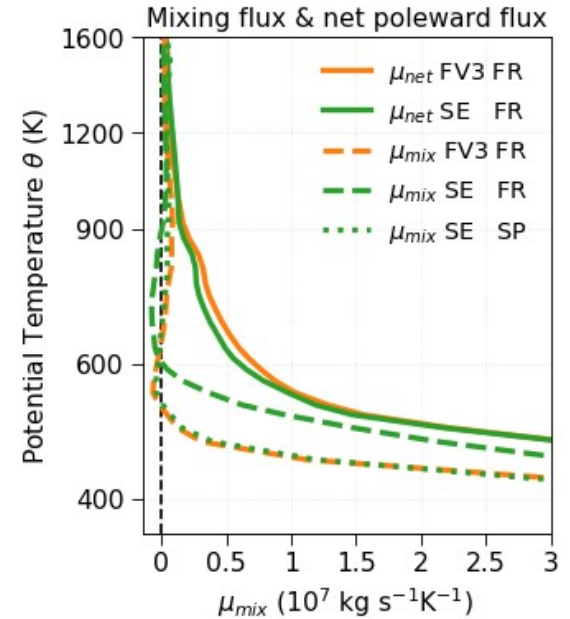
Higher mixing flux in CAM-SE as compared to GFDL-FV3

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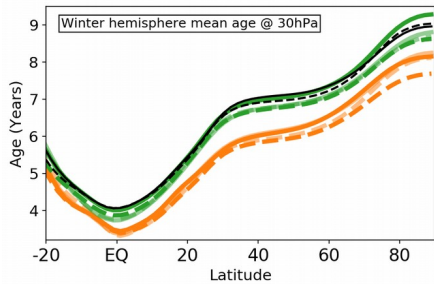
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- The tropical winds in the two models have different phases. Akin to different phases of the QBO.
- Westerlies induce more mixing between the two regions by allowing the midlatitude mixing fluxes to percolate deeper into the tropics



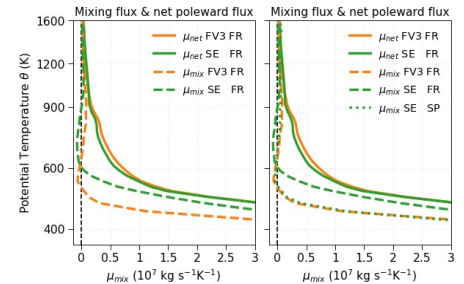
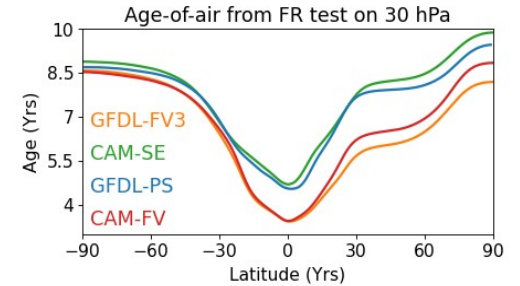
# Summary

Model numerics strongly influence the transport-dynamics coupling: finite-volume cores develop tropical easterlies while the spectral cores develop tropical westerlies (the FR test). Tropical differences strongly impact transport throughout the stratosphere, with age in CAM-SE being upto 40% older than in GFDL-FV3.



Constraining tropical winds, through nudging significantly reduces model age differences (the SP test). The models begin to show signs of convergence, although towards different values.

Equatorward shift in Rossby critical lines by a westerly jet enhances mixing of older midlatitude age and younger tropical air, increasing mean residence times of trace gases throughout the winter hemisphere.



## References

- Gupta, Aman, Edwin P. Gerber, and Peter H. Lauritzen (2020): “**Numerical impacts on tracer transport: A proposed intercomparison test of Atmospheric General Circulation Models**”, Quart. J. Roy. Meteor. Soc.
- Gupta, Aman, Edwin P. Gerber, R. Alan Plumb, and Peter H. Lauritzen (2021): “**Numerical impacts on tracer transport: Diagnosing the influence of dynamical core formulation and resolution on stratospheric transport**”, J. Atmos. Sci.,
- Linz, Marianna, R. Alan Plumb, Aman Gupta, and Edwin P. Gerber (2021) : “**Stratospheric adiabatic mixing rate derived from the vertical age gradient**”, J. Geophys. Res.: Atmospheres

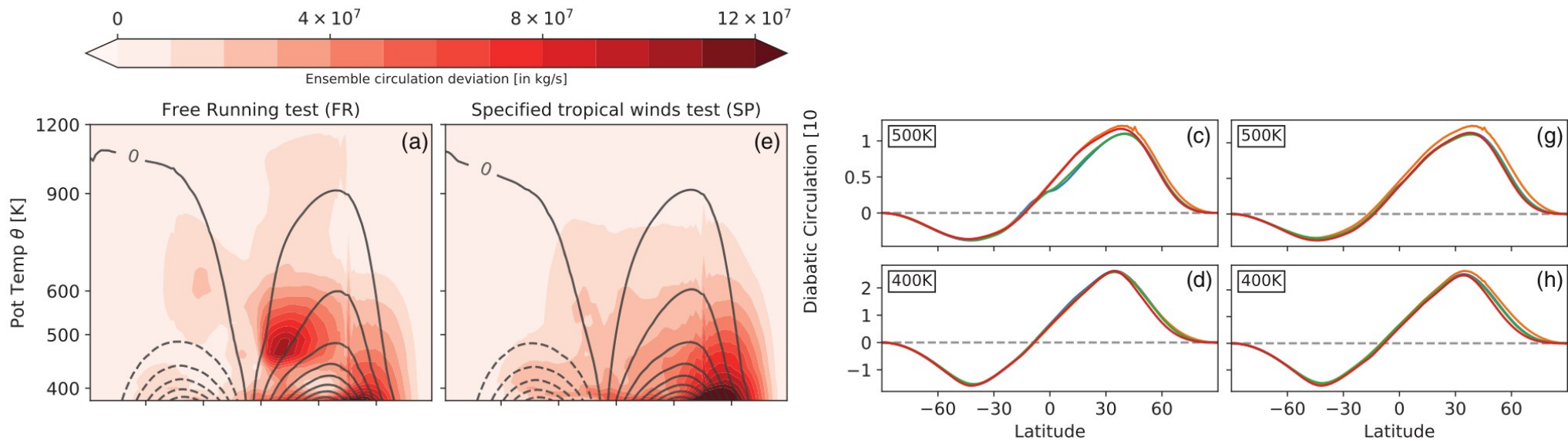
# Supplementary Plots

# Numerical Schemes

**TABLE A1** Horizontal and vertical tracer advection schemes employed by the four dynamical cores considered in the study

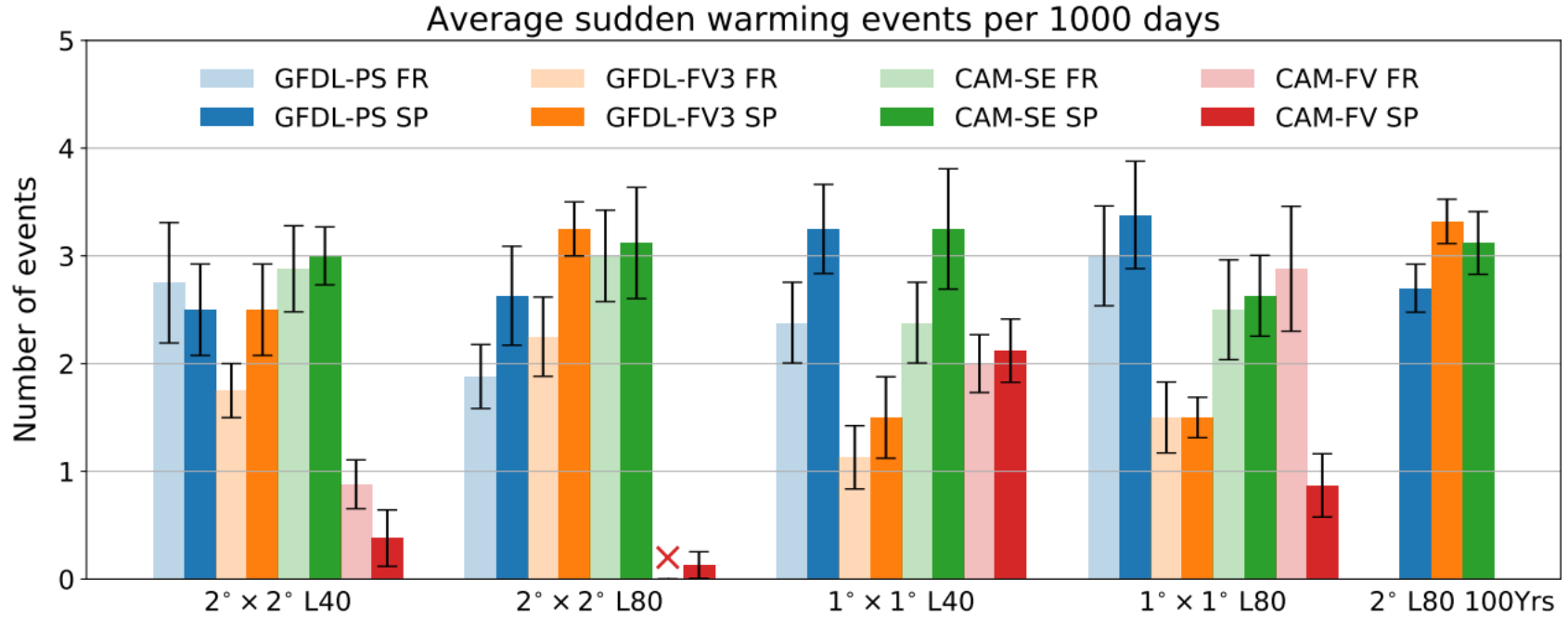
<b>Numerics</b>	<b>Horizontal tracer advection</b>	<b>Vertical tracer advection</b>
GFDL–Pseudospectral	Default Spectral Scheme	Piecewise Parabolic Method (Colella and Woodward, 1984)
GFDL–Cubed-Sphere Finite-Volume (GFDL-FV3)	Positive Definite Scheme as in Lin and Rood (1996) with Huynh constraint	Lin (2004) Vertically Lagrangian scheme. Remapping by monotonic and conservative cubic splines.
CAM–Spectral Element	Spectral Elements	Lin (2004) Vertically Lagrangian scheme. PPM vertical remapping with mirroring at boundaries.
CAM–Finite-Volume	<i>Enhanced</i> Piecewise Parabolic Method (PPM) (Colella and Woodward, 1984; Carpenter <i>et al.</i> , 1990)	<i>Enhanced</i> Piecewise Parabolic Method (PPM) (Colella and Woodward, 1984; Carpenter <i>et al.</i> , 1990)

# Intermodel Spread in Diabatic Circulation

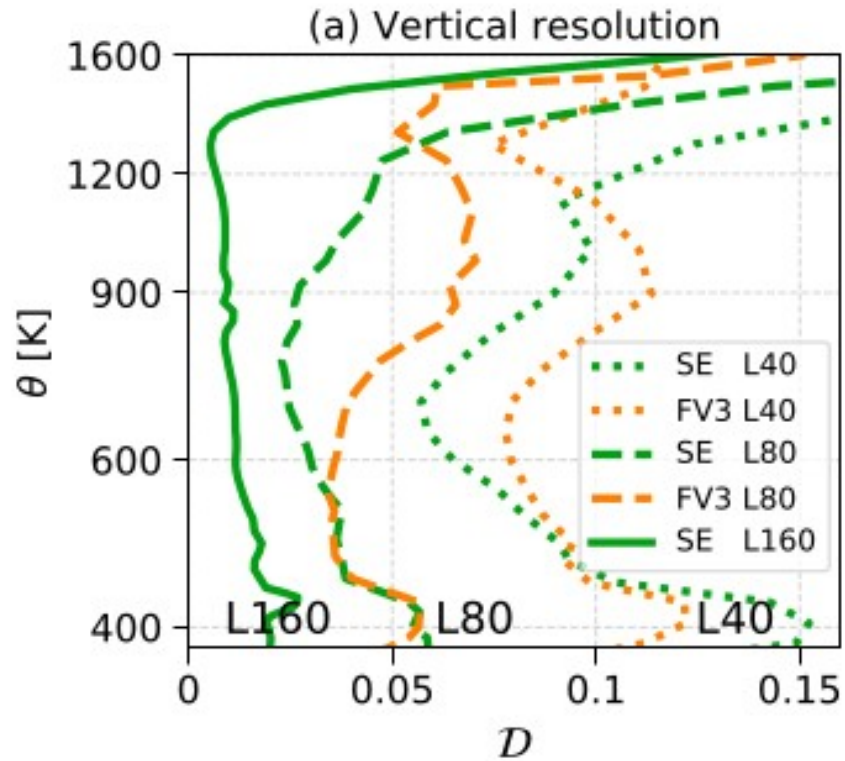




# SSW Frequency

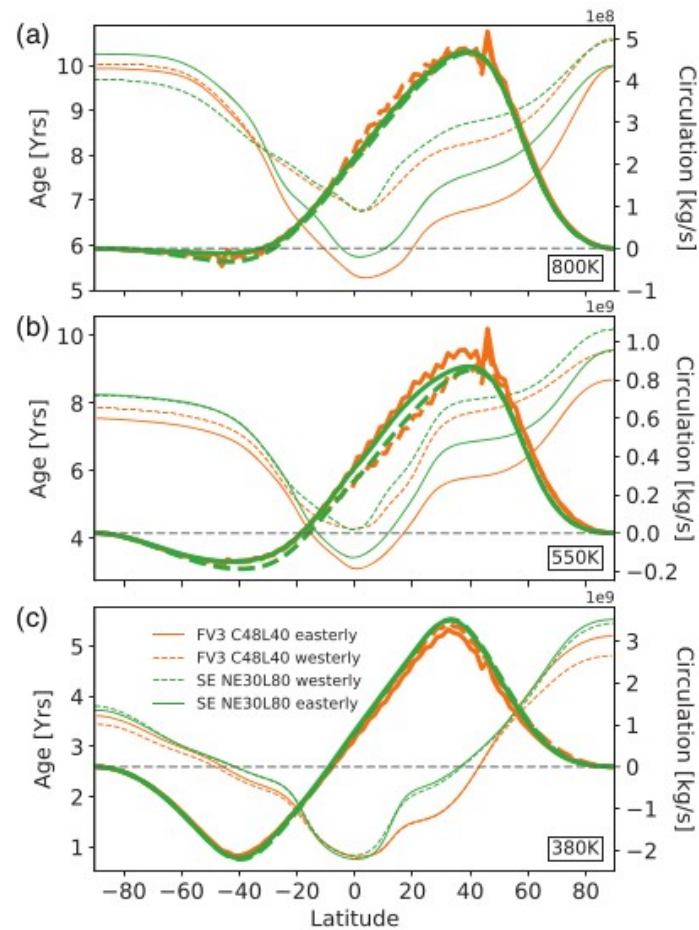


## Contribution from Vertical Diffusion



$$\mathcal{D} = \frac{\Gamma_u + \Gamma_d \left( \frac{M}{\Delta\Gamma} - \mathcal{M} \right)}{\mathcal{M}_u \Gamma_u + \mathcal{M}_d \Gamma_d}.$$

# Imposing a tropical westerly jet in the GFDL-FV3 model



# Imposing a tropical westerly jet in the GFDL-FV3 model

